



International  
Centre for  
Radio  
Astronomy  
Research

# Methods for mm-VLBI using Multi-Frequency Observations

*Maria J. Rioja*  
*ICRAR (Australia), OAN (Spain)*

*Richard Dodson*  
*ICRAR (Australia)*



Curtin University



THE UNIVERSITY OF  
WESTERN AUSTRALIA



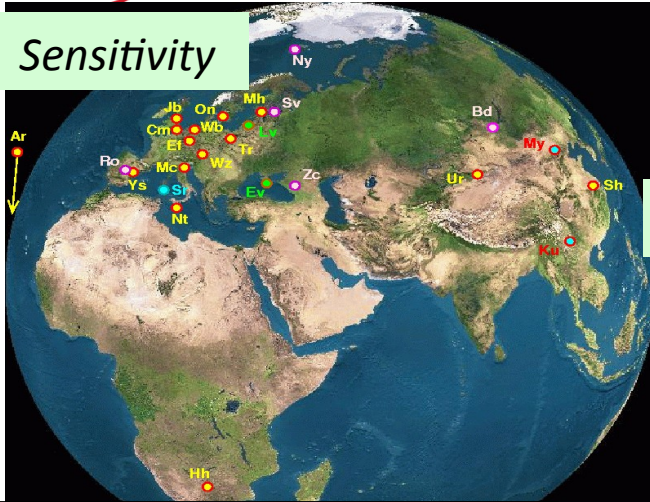
# Overview

- Context
- A mm-VLBI method: SOURCE FREQUENCY PHASE REFERENCING (SFPR)
  - ➔ Outcomes: 1) Effective Atmospheric Compensation,  
2) Increased Sensitivity, and  
3) Astrometry
- Empirical Demonstration with multi-frequency observations with the Korean VLBI Network, up to 132 GHz
- Work-in-progress and what's next?



# VLBI NETWORKS

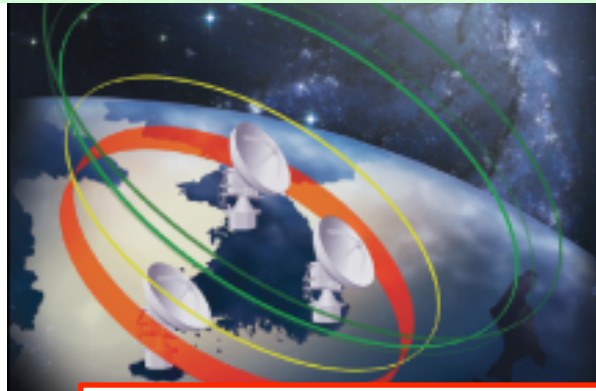
## Sensitivity



**EVN: European VLBI Network**

<~ 22GHz

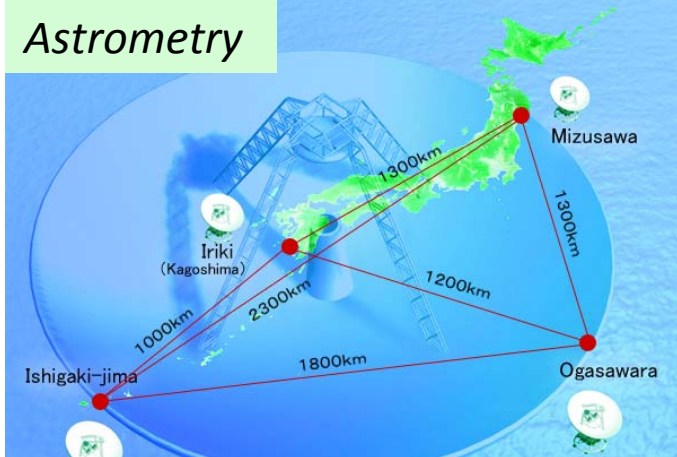
## Highest Frequency Astrometry



**KVN Korean VLBI Network**

22/43/86/129 GHz

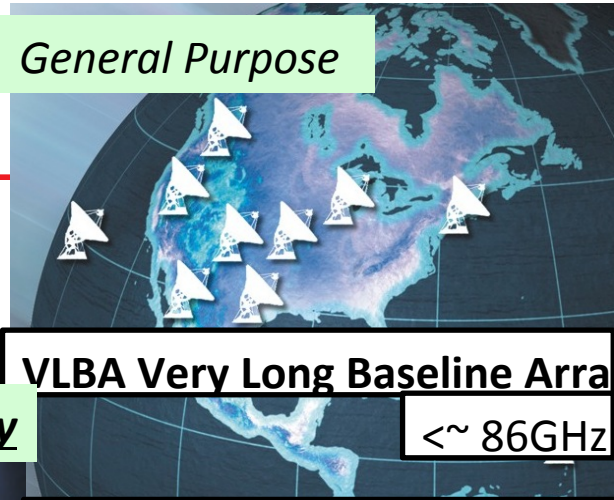
## Astrometry



**VERA VLBI for Earth Rotation and Astrometry**

22/43 GHz

## General Purpose



**VLBA Very Long Baseline Array**

<~ 86GHz

**GMVA Global mm VLBI Array**

86GHz



## Southern Hemisphere



**LBA Long Baseline Array**

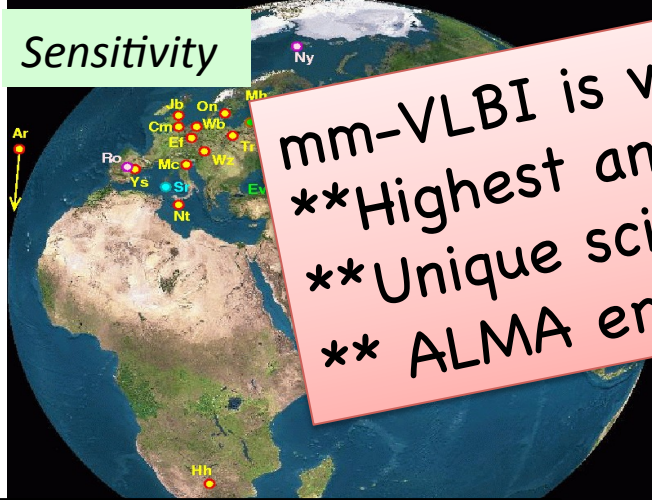
<~ 22GHz





# VLBI NETWORKS

Sensitivity

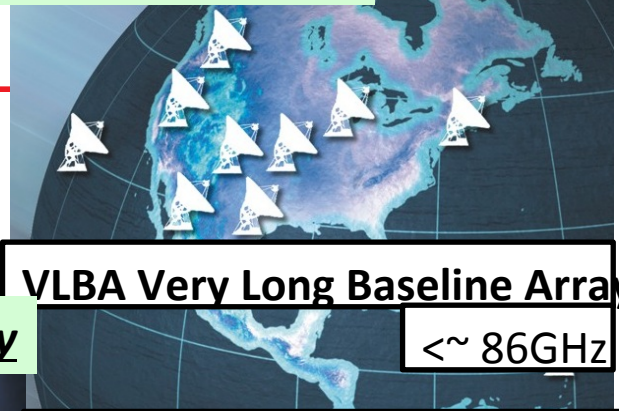


EVN: European VLBI Network

<~ 22GHz

mm-VLBI is very interesting!  
\*\* Highest angular resolution  
\*\* Unique science  
\*\* ALMA era

General Purpose



VLBA Very Long Baseline Array

<~ 86GHz

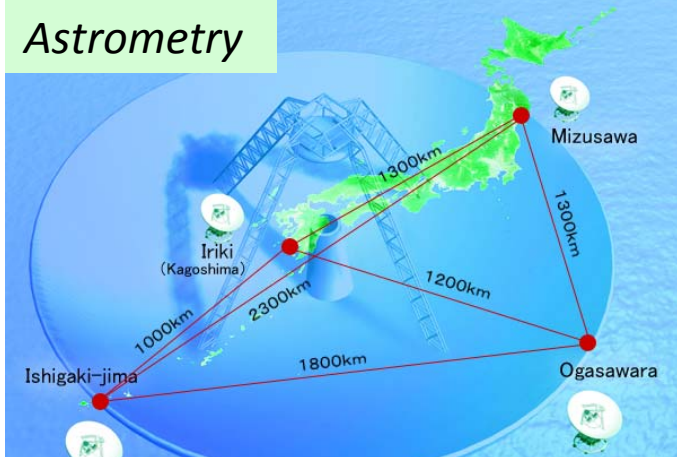
Astrometry

GMVA Global mm VLBI Array

86GHz



Astrometry



KVN Korean VLBI Network

22/43/86/129 GHz

Southern Hemisphere



LBA Long Baseline Array

<~ 22GHz

and Space Science Institute

VERA VLBI for Earth Rotation and Astrometry

22/43 GHz

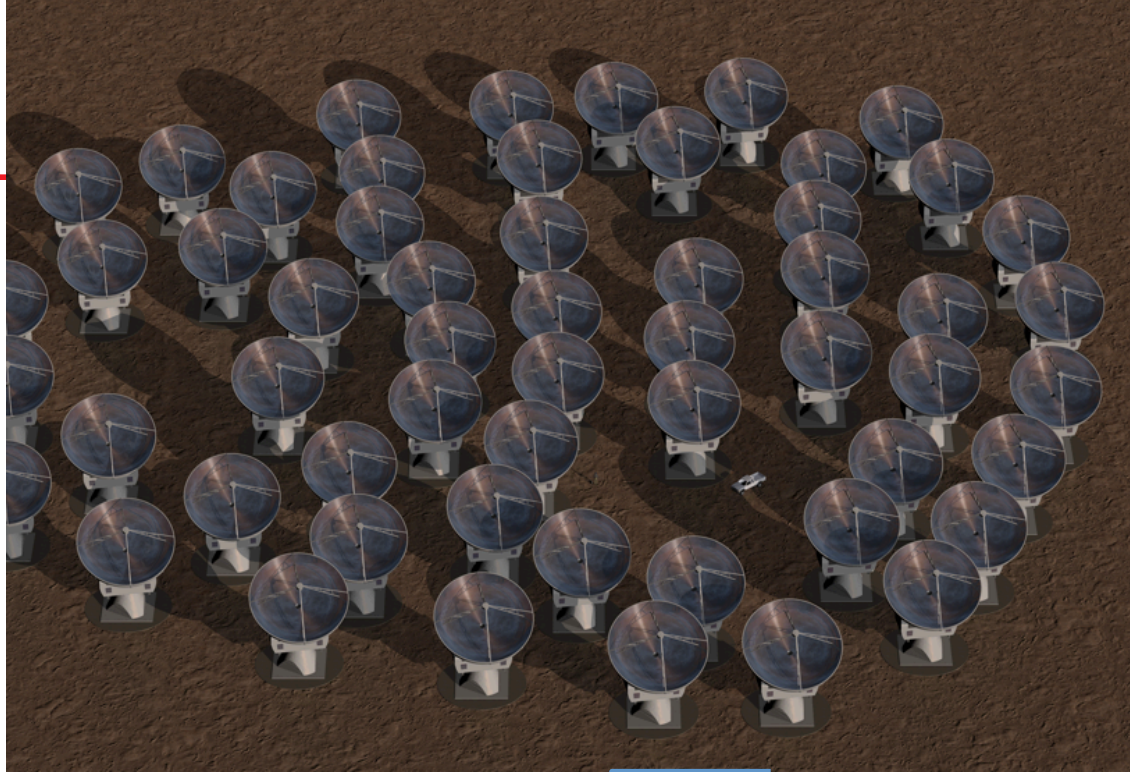


# But mm-VLBI is challenging...

## Limited Sensitivity:

- Limited aperture efficiency
- Receiver system temperatures
- Rapid tropospheric fluctuations  $\propto \nu$
- Short tropospheric coherence time
- Sources intrinsically weaker, in general

HANDFUL OF TARGETS



Improve Performance by reducing threshold of detected flux ( $\Delta S$ ):

$$\Delta S_{ij} = \frac{1}{\eta_s} \times \sqrt{\frac{SEFD_i \times SEFD_j}{2 \times \Delta \nu \times \tau_{\text{Coh.}}}}$$

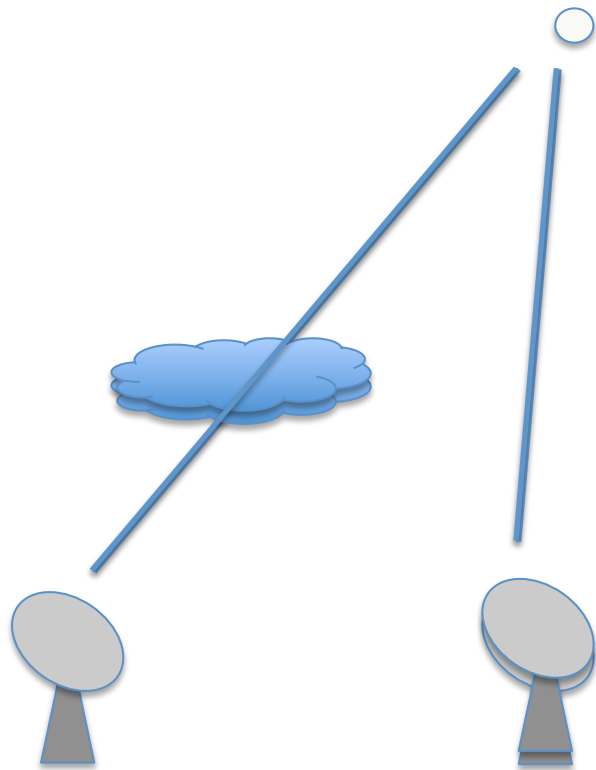
Smaller SEFD through Huge Collecting Area,

INCREASING coherent Integration Time Through superior tropospheric calibration

GOAL: Higher sensitivity → wider applicability

# Phase Referencing “*trans-source*”

PR @ 22 GHz



Weak Target  
Source

**AIM:** Improve performance of cm-VLBI,  
1) Higher sensitivity (micro-Jy sources),  
2) high precision astrometry (micro-as)  
by correcting for tropospheric fluctuations.

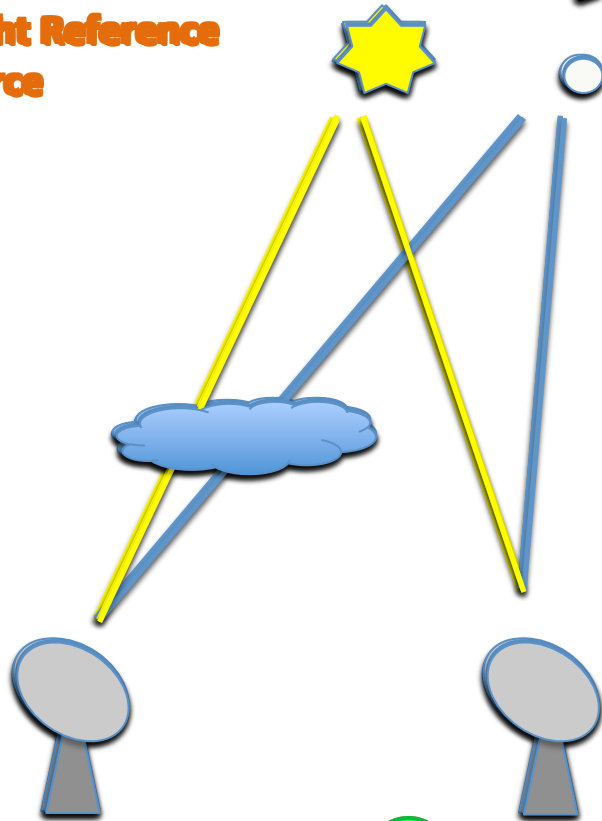
# Phase Referencing “trans-source”

PR @ 22 GHz

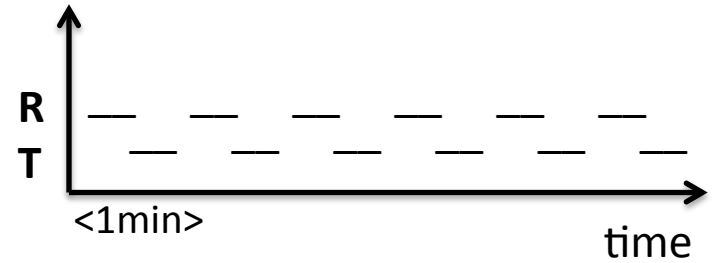
Bright Reference  
Source

~ 1 deg.

Weak Target  
Source



Duty Cycle @ 22 GHz



**AIM:** Improve performance of cm-VLBI,  
1) Higher sensitivity, and  
2) high precision astrometry  
by correcting for tropospheric fluctuations.

## **STRATEGY:**

1) Use interleaving observations of a nearby **reference source** to correct for the errors  
And then coherently add the signal of the **Target source** beyond trop. coherence time.

2) Temporal and Spatial interpolation.

3) Telescope switching fully samples tropospheric changes

WEAK SOURCES  
ASTROMETRY





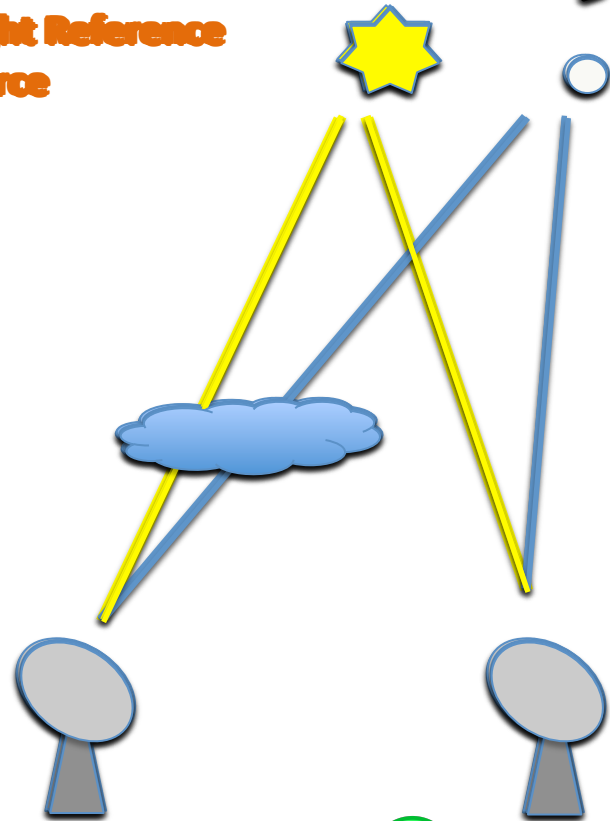
# Phase Referencing “trans-source”

PR @ 43 GHz

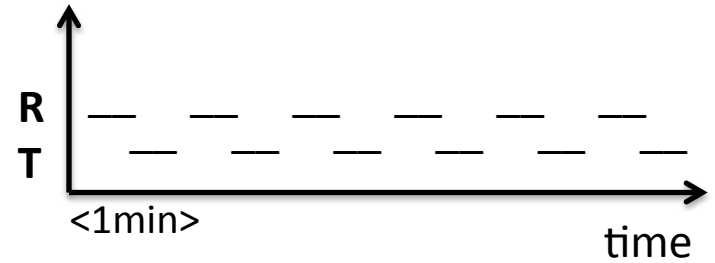
Bright Reference Source

~ 1 deg.

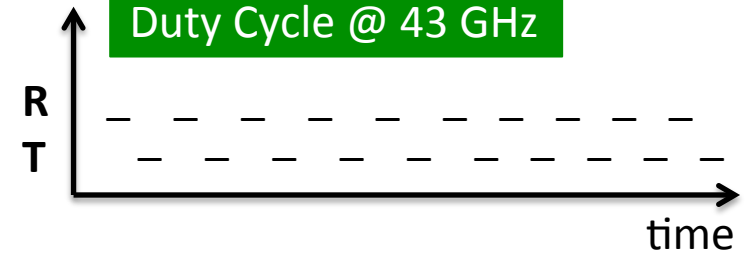
Weak Target Source



Duty Cycle @ 22 GHz



Duty Cycle @ 43 GHz



Limit on how fast a telescope can move constrains  
The application to 43 GHz or below (in general).

Defeated by rapid phase tropospheric fluctuations,  
linear increase with frequency (non-dispersive)

Limitations in performance start at freq. > 43 GHz

WEAK SOURCES  
ASTROMETRY

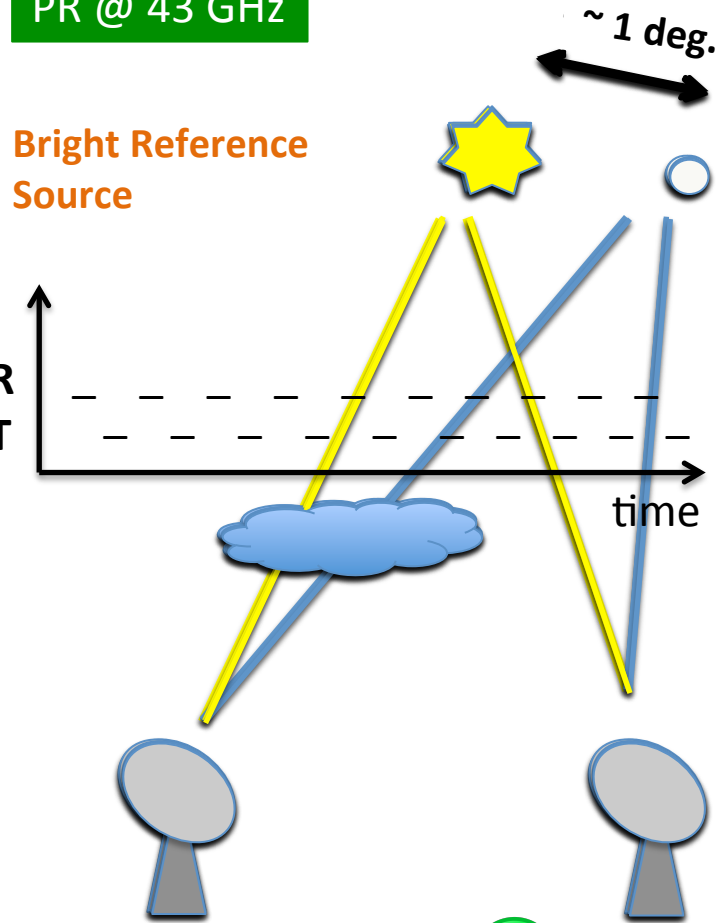


# Phase Referencing “trans-source”

# Paradigm Shift: “trans-frequency” calibration

“fast-frequency switching”  
with VLBA

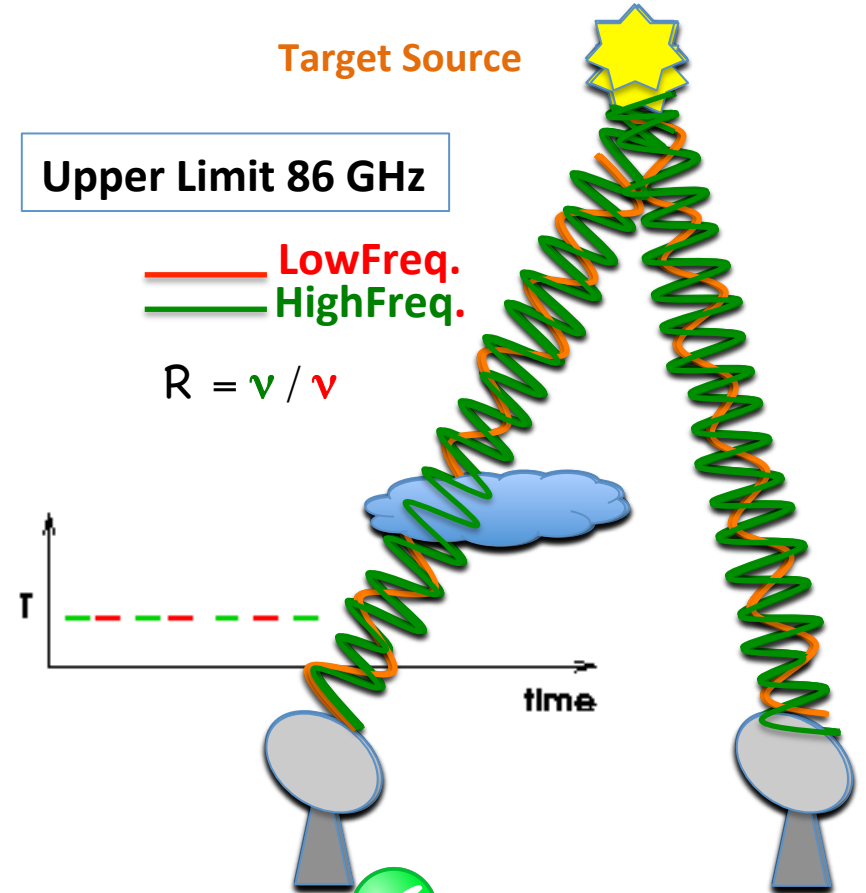
PR @ 43 GHz



WEAK SOURCES  
ASTROMETRY



Upper Limit 86 GHz



WEAK SOURCES  
ASTROMETRY

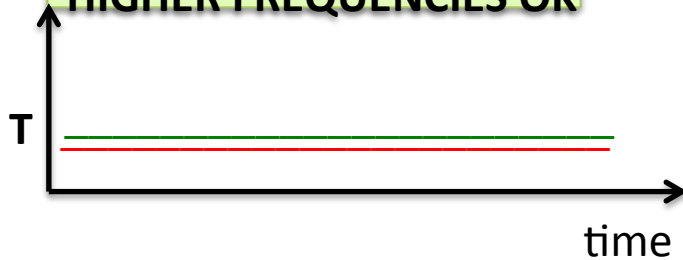


Middelberg et al. 2005  
Rioja & Dodson 2008, 2011

# ALTERNATIVE APPROACH FOR SUPERIOR TROPOSPHERIC COMPENSATION



**BETTER SIMULTANEOUS!  
HIGHER FREQUENCIES OK**



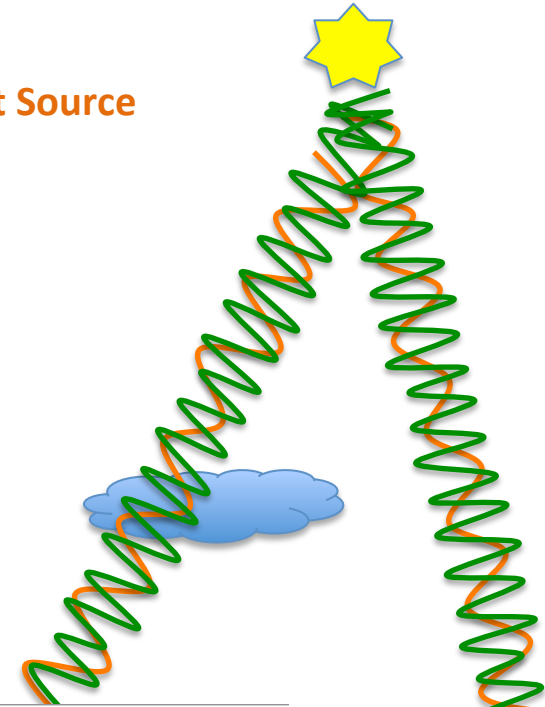
- 1) No interpolation is required
- 2) Applicable to higher frequencies

## Multi-Channel KVN receivers

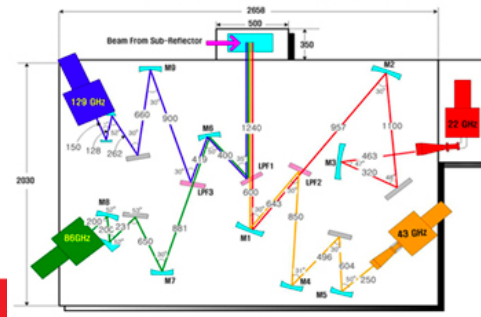
WEAK SOURCES  
ASTROMETRY



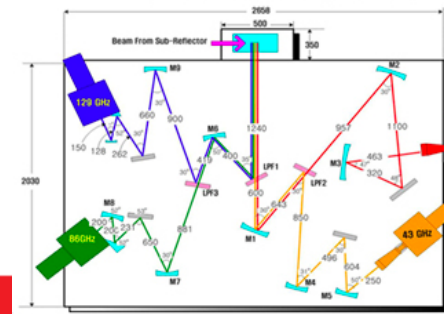
Target Source



KVN Multi-Channel Receiver Optical Bench



KVN Multi-Channel Receiver Optical Bench

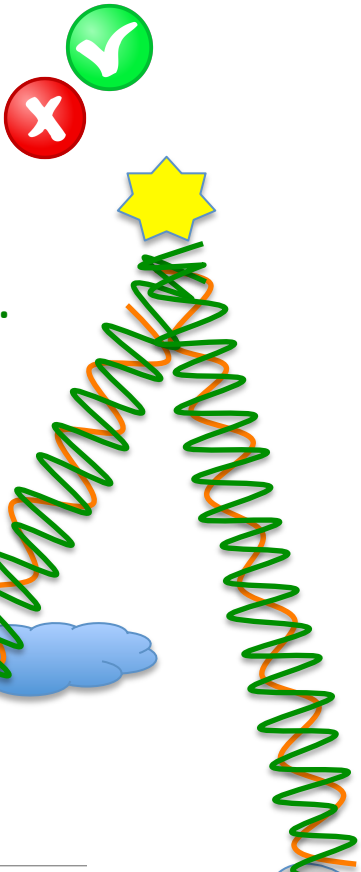






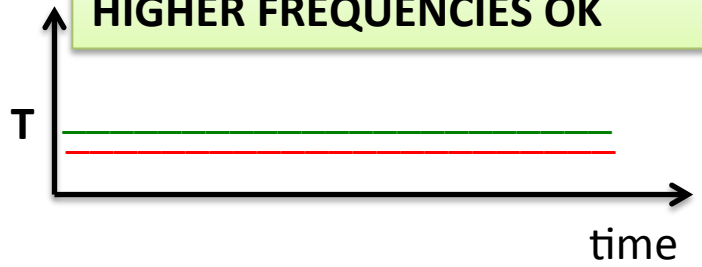
# Frequency Phase Referencing (FPT)

WEAK SOURCES  
ASTROMETRY



Target Source  
@low&high freq.

BETTER (near) SIMULTANEOUS!  
HIGHER FREQUENCIES OK

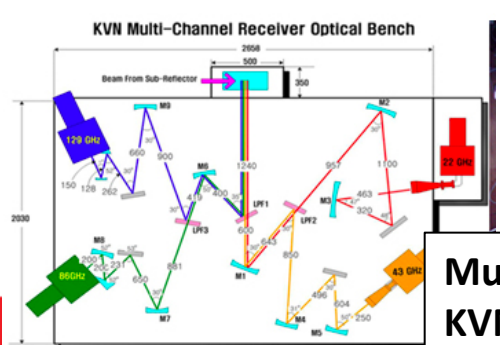
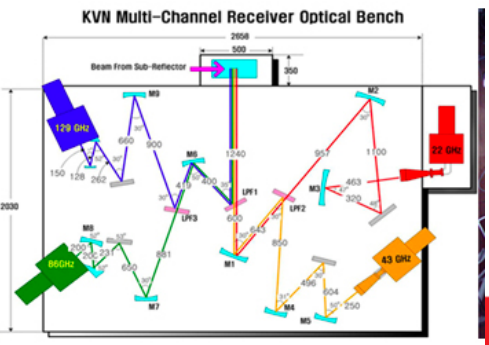


$$R = v / v$$

Fast Slow Slow

$$\phi_A = \phi_{A,GEO} + \phi_{A,TRO} + \phi_{A,ION} + \phi_{A,INST} + \phi_{A,STR} + 2\pi n_A$$

$$\phi_A = \phi_{A,GEO} + \phi_{A,TRO} + \phi_{A,ION} + \phi_{A,INST} + 2\pi n_A$$



Multi-channel  
KVN receivers

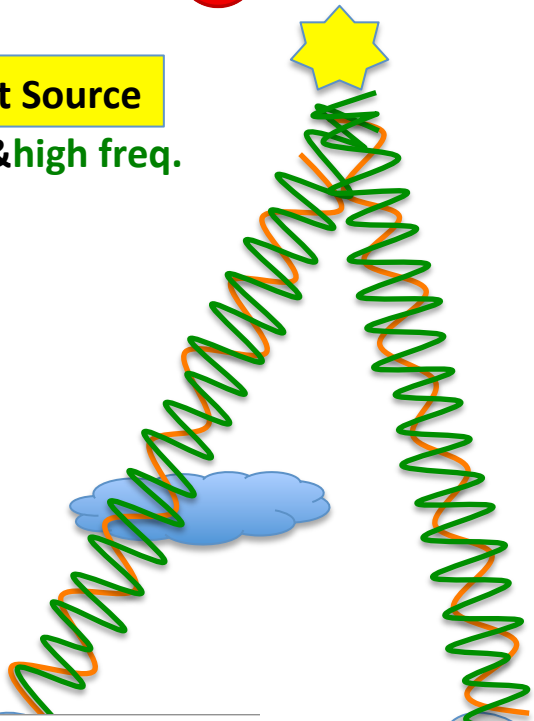


# Frequency Phase Referencing (FPT)

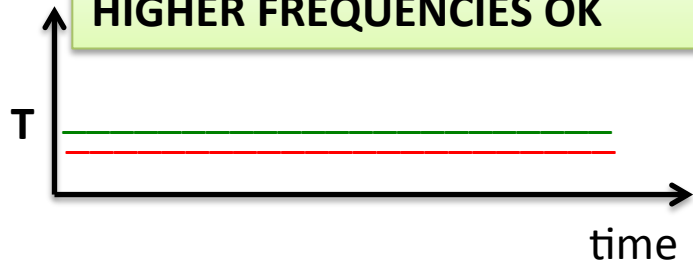
WEAK SOURCES  
ASTROMETRY



Target Source  
@low&high freq.



BETTER (near) SIMULTANEOUS!  
HIGHER FREQUENCIES OK



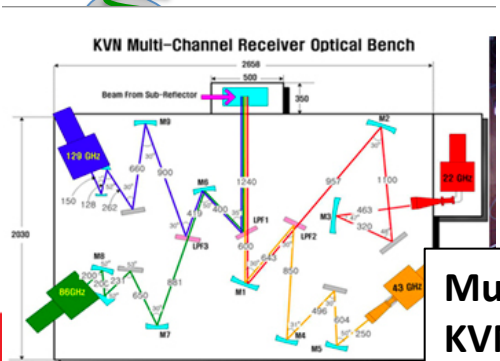
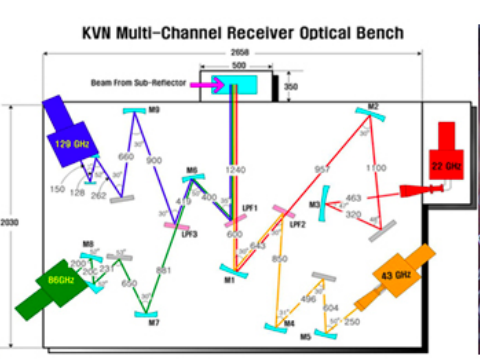
$$R = v / v$$

Fast Slow Slow



$$\phi_A = \phi_{A,GEO} + \phi_{A,TRO} + \phi_{A,ION} + \phi_{A,INST} + \phi_{A,STR} + 2\pi n_A$$

$$R * \phi_A = R * (\phi_{A,GEO} + \phi_{A,TRO} + \phi_{A,ION} + \phi_{A,INST} + \hat{2\pi n_A})$$



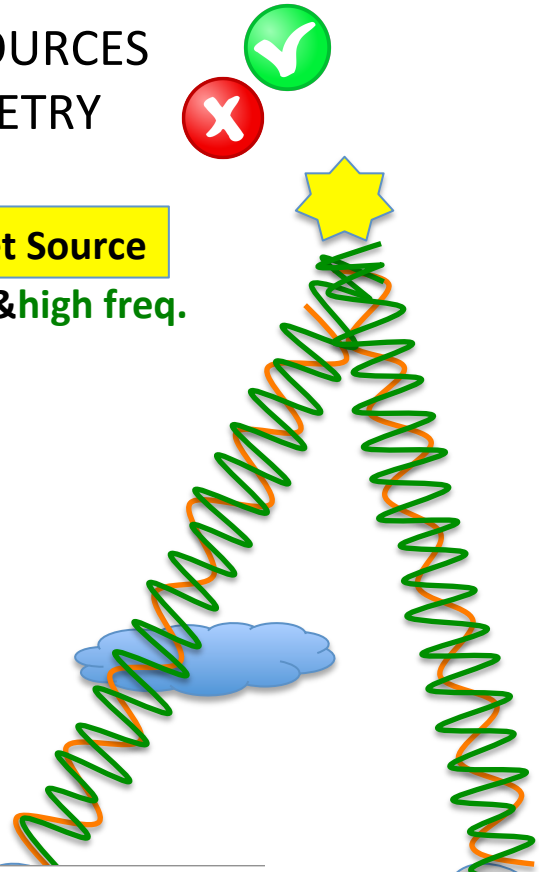
Multi-channel  
KVN receivers



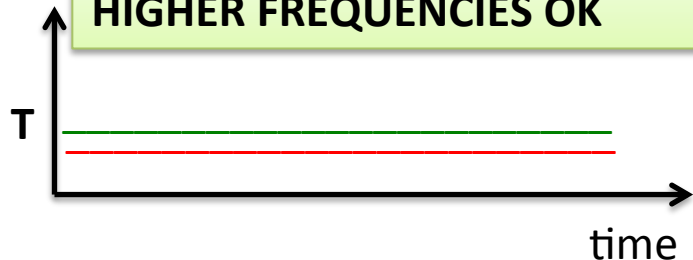
# Frequency Phase Referencing (FPT)

WEAK SOURCES  
ASTROMETRY

Target Source  
@low&high freq.



BETTER (near) SIMULTANEOUS!  
HIGHER FREQUENCIES OK



$$R = v / \nu$$

Fast    Slow    Slow

$$\phi_A^{FPT} = \cancel{\phi_{A,GEO}} + \cancel{\phi_{A,TRO}} + \phi_{A,ION} + \phi_{A,INST} + \phi'_{A,STR} + 2\pi n_A$$

$$R * \phi_A = R * (\phi_{A,GEO} + \phi_{A,TRO} + \phi_{A,ION} + \phi_{A,INST} + \hat{2\pi n_A})$$

Non-dispersive Errors:

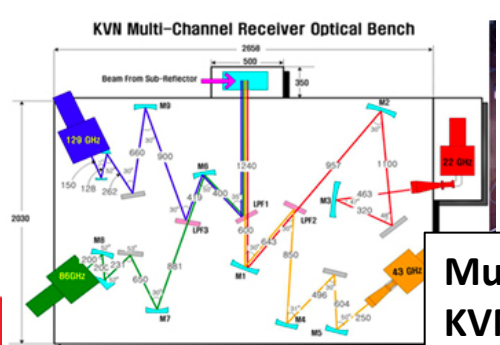
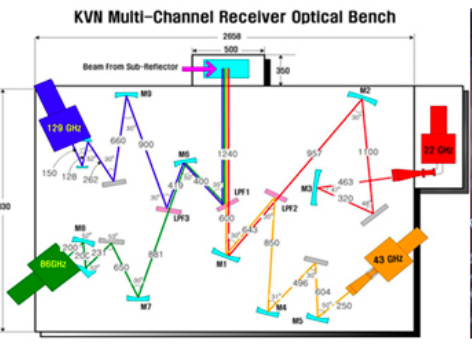
$$\phi_{A,TRO} - R * \phi_{A,TRO} = 0$$

$$\phi_{A,GEO} - R * \phi_{A,GEO} = 0$$

Dispersive Errors:

$$\phi_{A,ION} - R * \phi_{A,ION} = (R-1/R) * \phi_{A,ION}$$

$\phi_{A,INST}$  ... Anything!



Multi-channel  
KVN receivers





# Frequency Phase Referencing (FPT)

**OUTCOME:** **PRECISE CALIBRATION OF THE TROPOSHERE**  
(and in general any non-dispersive residuals)

**ENABLES:** **EXTENDED COHERENCE TIME**

- ➔ **WEAK SOURCE DETECTION AT HIGH FREQUENCIES**
- ➔ **~~ASTROMETRY~~**

*\* (near) SIMULTANEOUS multi-frequency observations required for high freqs.*

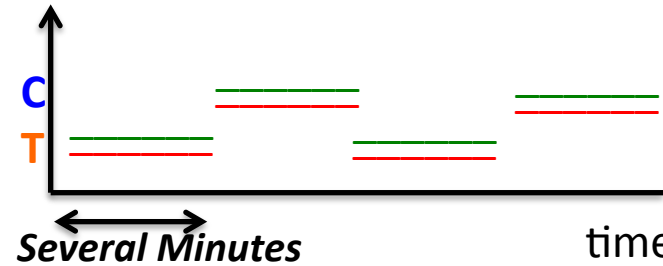


# The Quest of Astrometry...

## Source Frequency Phase Referencing (SFPR)

SFPR: Rioja & Dodson '08,'11,'14,'15

**(TWO SOURCES)**



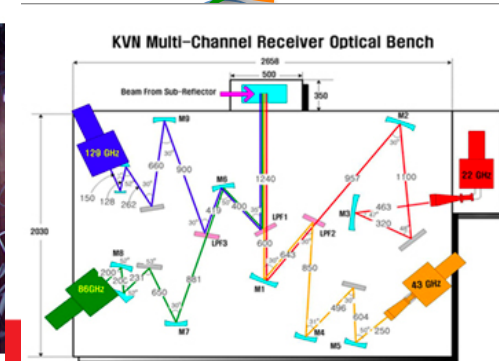
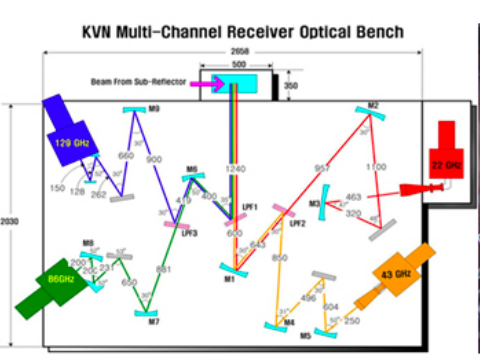
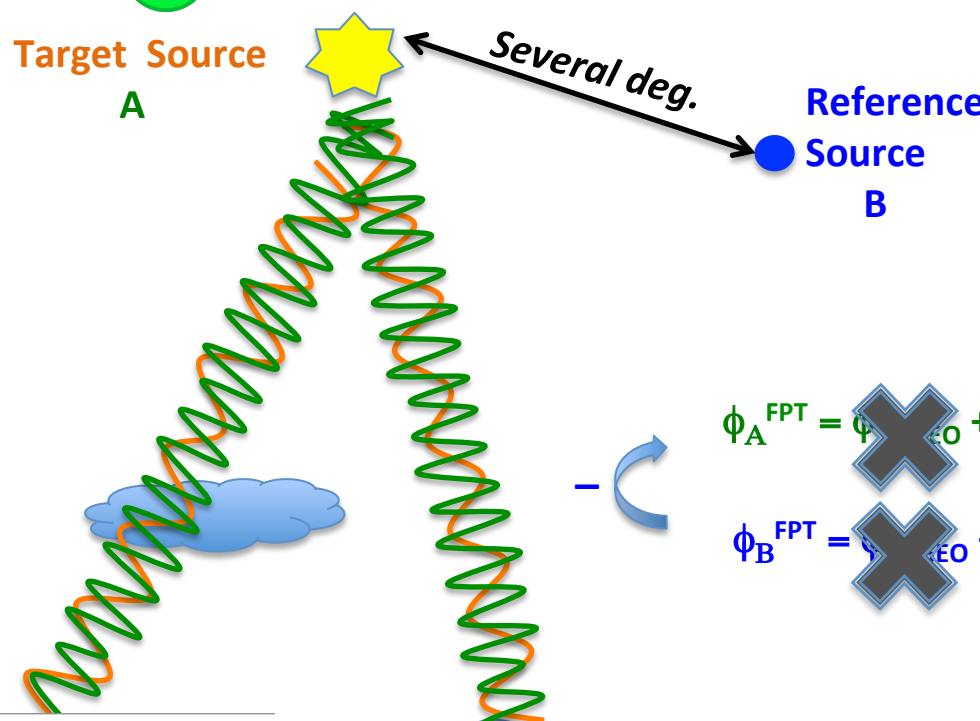
$$R = v / \nu$$

Fast Slow Slow

$$\phi_A^{FPT} = \cancel{\phi_{A,EO}} + \cancel{\phi_{A,IO}} + \phi_{A,ION} + \phi_{A,INST} + \phi_{A,STR} + 2\pi n_A$$

$$\phi_B^{FPT} = \cancel{\phi_{B,EO}} + \cancel{\phi_{B,IO}} + \phi_{B,ION} + \phi_{B,INST} + \phi_{B,STR} + 2\pi n_B$$

WEAK SOURCES   
ASTROMETRY



KVN



# The Quest of Astrometry...

## Source Frequency Phase Referencing (SFPR)

SFPR: Rioja & Dodson '08,'11,'14,'15

(TWO SOURCES)

WEAK SOURCES

ASTROMETRY

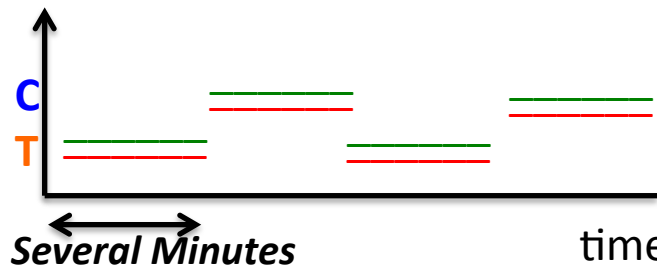
Target Source A

A

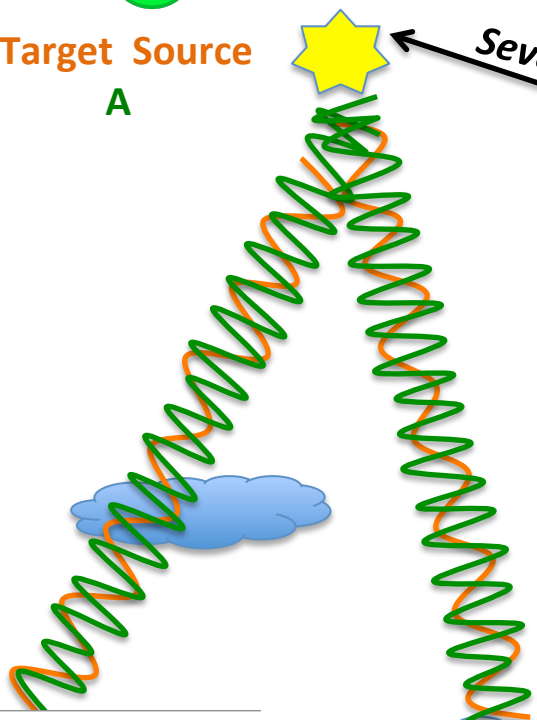
Several deg.

Reference Source B

B



$$R = \frac{v}{v}$$



$$\phi_{A-B}^{SFPR} = \cancel{\phi_{A,EO}} + \cancel{\phi_{A,IO}} + \cancel{\phi_{A,IN}} + \cancel{\phi_{A,ST}} + \phi'_{A,STR} + 2\pi n_A$$

$$\phi_B^{FPT} = \cancel{\phi_{B,EO}} + \cancel{\phi_{B,IO}} + \phi_{B,ION} + \phi_{B,INST} + \phi'_{B,STR} + 2\pi n_B$$

Fast Slow Slow

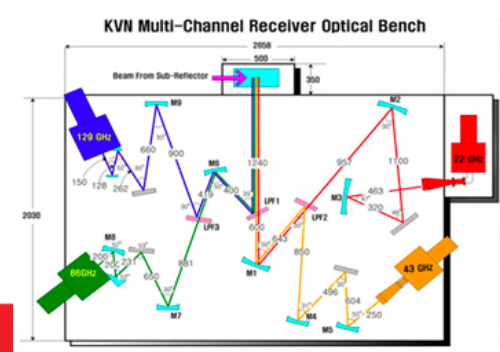
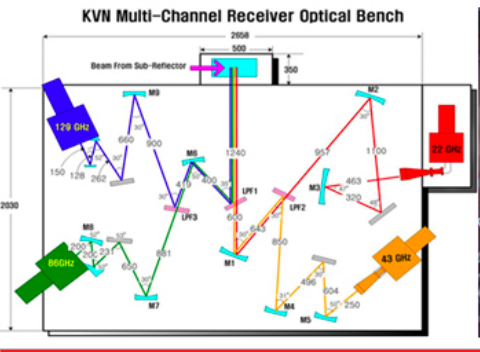
$$\phi_{A,ION} - \phi_{B,ION} = 0$$

$$\phi_{A,INST} - \phi_{B,INST} = 0$$

Astrometry:

$$\phi_{A-B}^{SFPR} \xleftrightarrow{FFT} \text{SFPRed A-Map at high freq.}$$

KVN







**OUTCOME:** PRECISE ATMOSPHERIC & INSTR. CALIBRATION,  
WHILE KEEPING ASTROMETRIC SIGNATURE

**ENABLES:** EXTEND COHERENCE TIME & ASTROMETRY AT HIGH FREQS

- ➔ WEAK SOURCE DETECTION
- ➔ ASTROMETRY (frequency dependent position shifts:  
continuum & lines; registration of images at multiple  
frequencies)

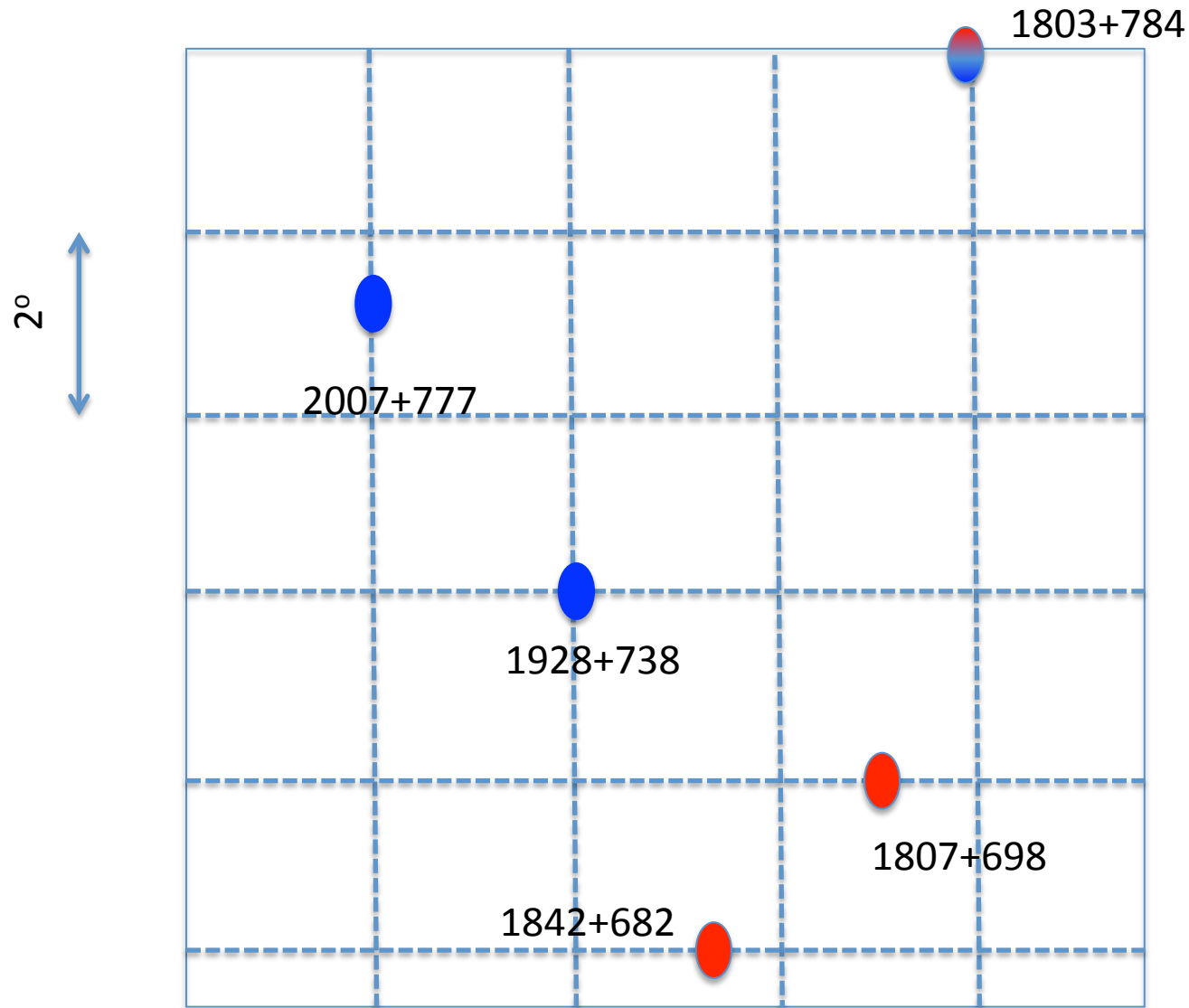
\*Slow antenna switching OK

\*Several degrees source separation OK

\* *(near)SIMULTANEOUS multi-frequency observations required for high freqs.*



# Empirical Demonstration: 4-band KVN SFPR observations of 5 AGNs



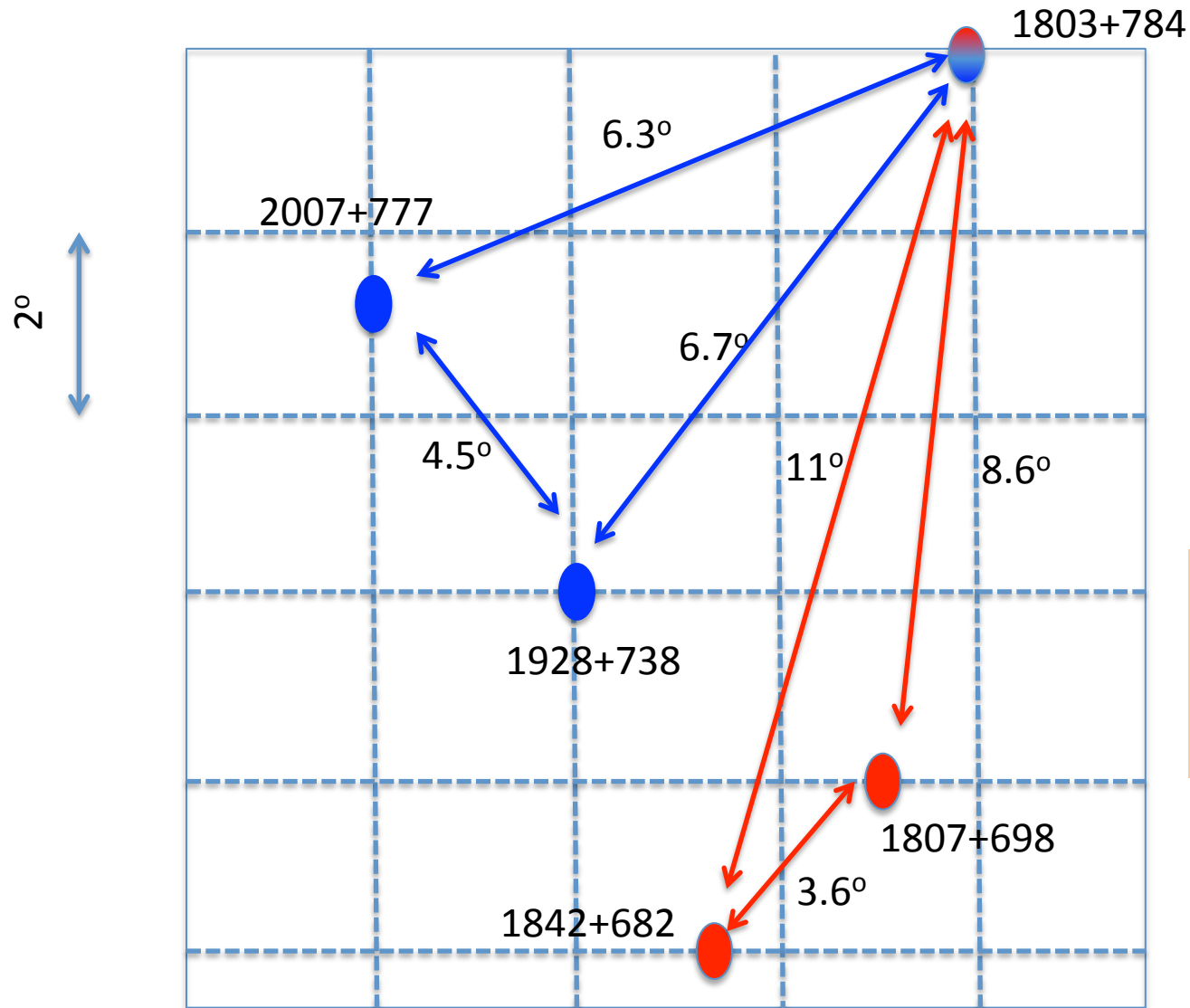
Triangle 1  
Triangle 2

22,43,86,130 GHz  
K,Q,W,D bands

(Rioja,Dodson+'15)



# Empirical Demonstration: 4-band KVN SFPR observations of 5 AGNs



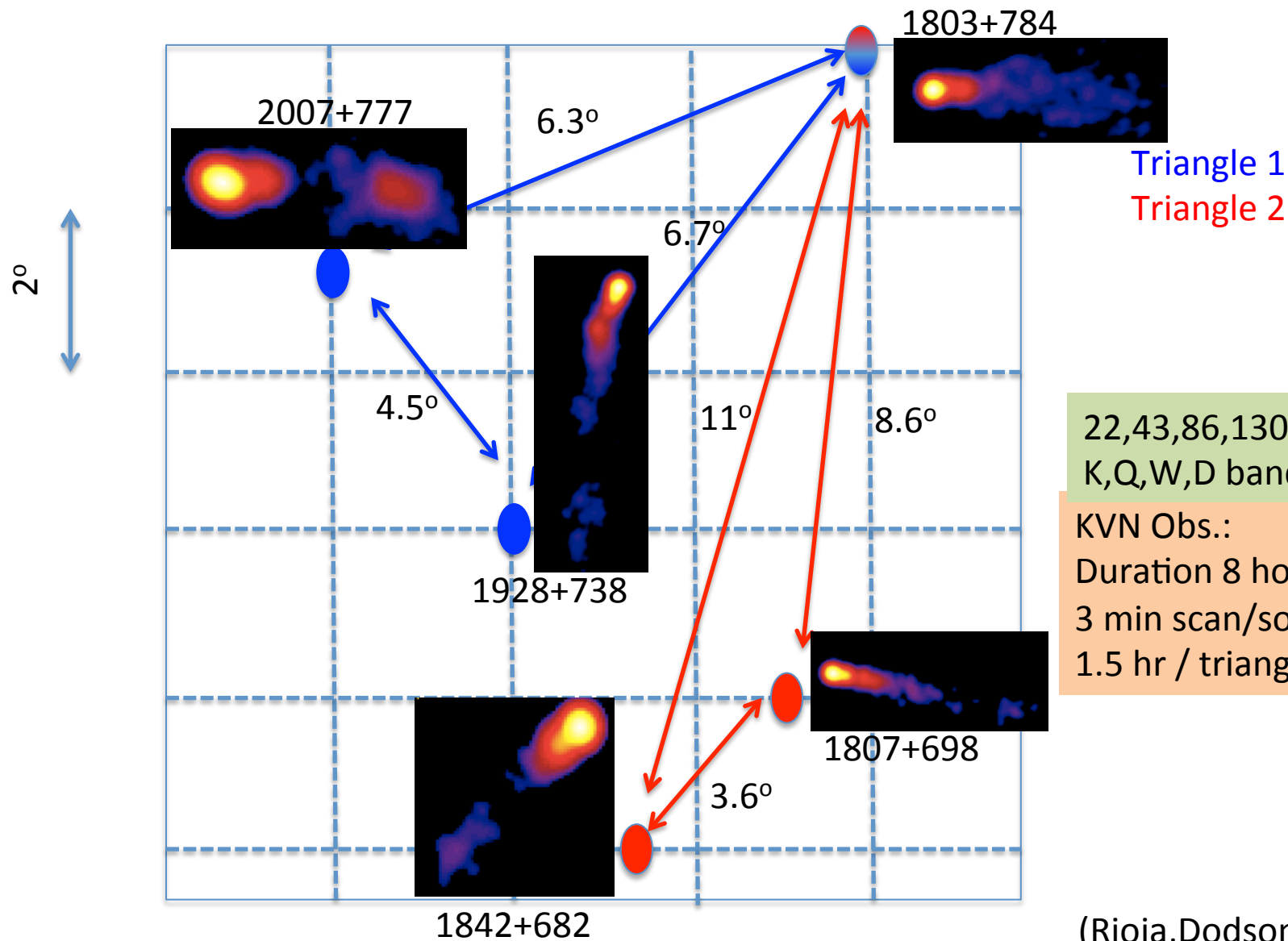
Triangle 1  
Triangle 2

22,43,86,130 GHz  
K,Q,W,D bands

KVN Obs.:  
Duration 8 hours  
3 min scan/source  
1.5 hr / triangle

(Rioja,Dodson+'15)

# Empirical Demonstration: 4-band KVN SFPR observations of 5 AGNs

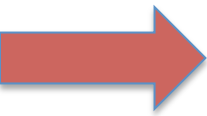


(Rioja, Dodson+ '15)



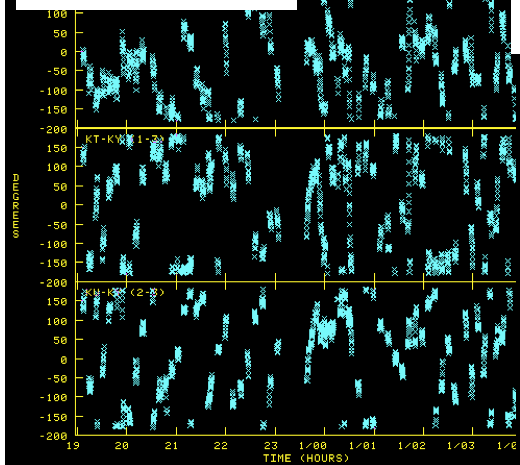


# Empirical Demonstration: 4-band KVN SFPR observations of 5 AGNs

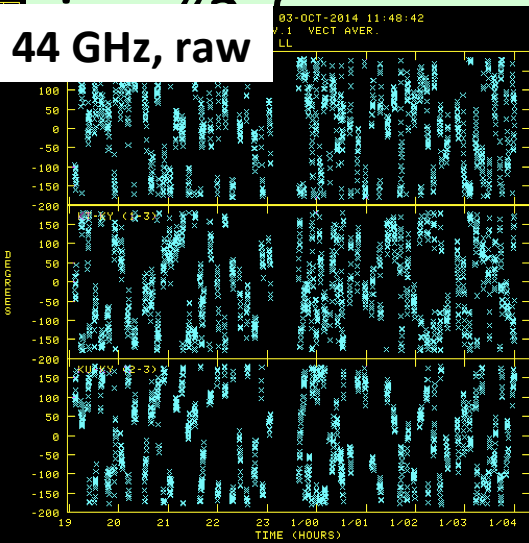


(1) Outcomes: Effective Tropospheric Compensation  
**FPT analysis – “2-frequencies”**

22 GHz, raw



44 GHz, raw

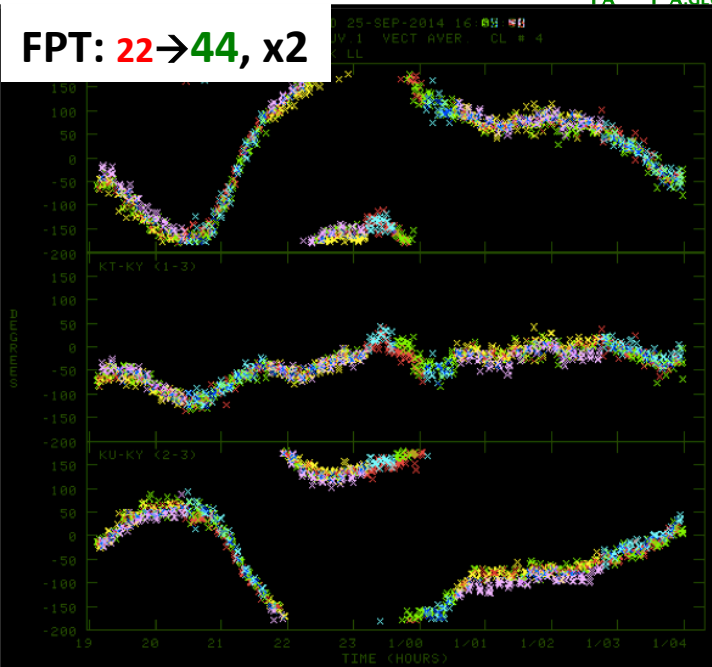


ies”  
for a given  $\nu_{\text{low}}$  (22GHz)

$$\phi_A = \phi_{A,\text{GEO}} + \phi_{A,\text{TRO}} + \phi_{A,\text{ION}} + \phi_{A,\text{INST}} + 2\pi n$$

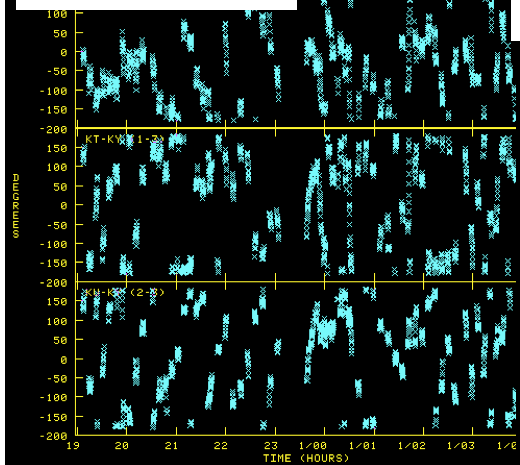
$$\phi_A = \phi_{A,\text{GEO}} + \phi_{A,\text{TRO}} + \phi_{A,\text{ION}} + \phi_{A,\text{INST}} + 2\pi n_A$$

FPT: 22→44, x2

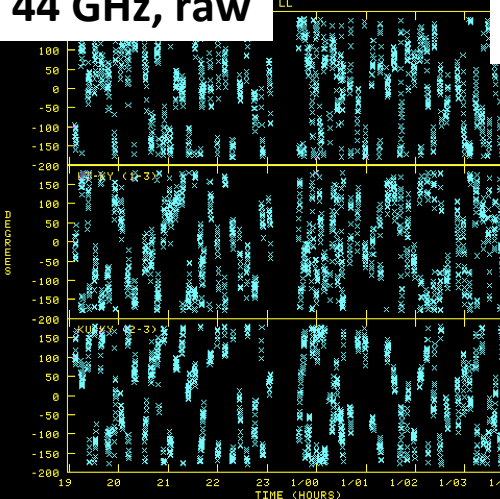


$$\phi_A - 2 * \phi_A$$

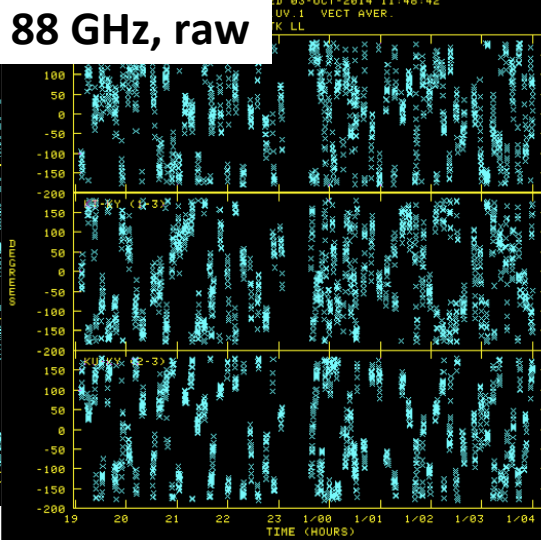
22 GHz, raw



44 GHz, raw



88 GHz, raw

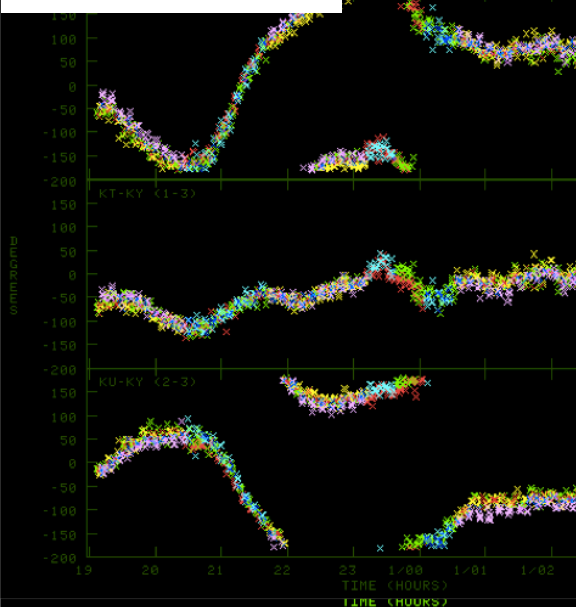


2GHz)

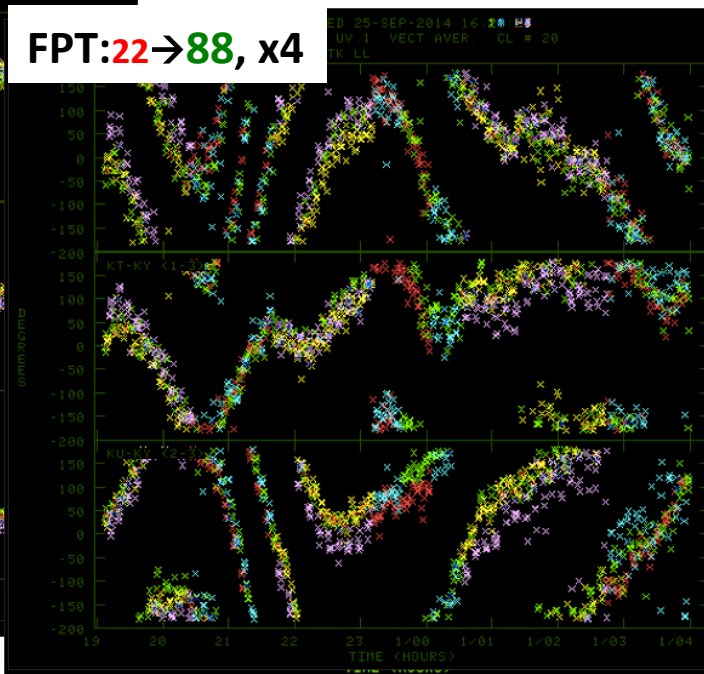
$$\phi_A = \phi_{A,GEO} + \phi_{A,TRO} + \phi_{A,ION} + \phi_{A,INST} + 2\pi t$$

$$\phi_A = \phi_{A,GEO} + \phi_{A,TRO} + \phi_{A,ION} + \phi_{A,INST}$$

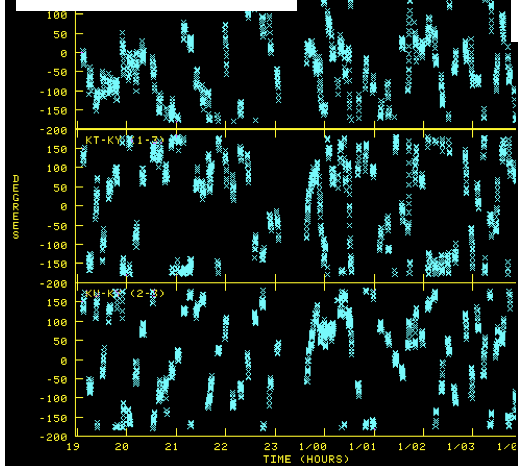
FPT: 22→44, x2



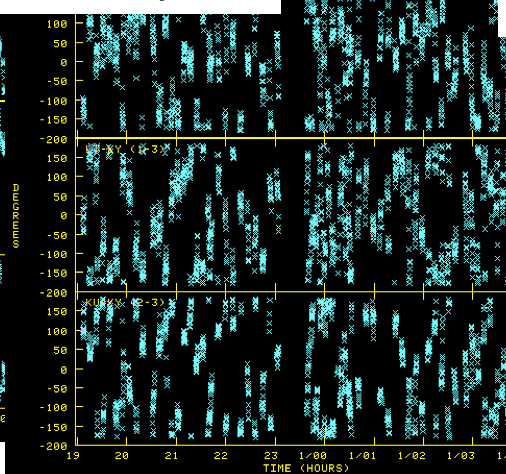
FPT: 22→88, x4



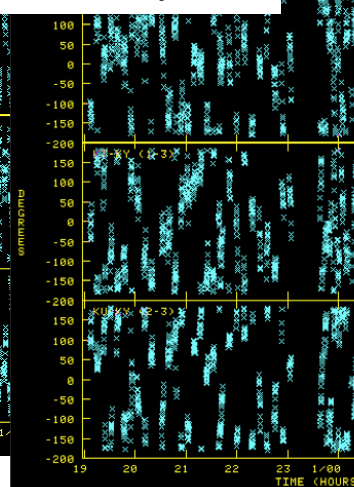
22 GHz, raw



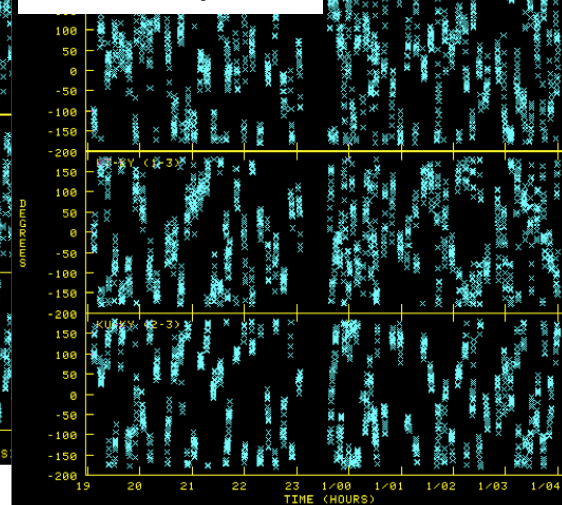
44 GHz, raw



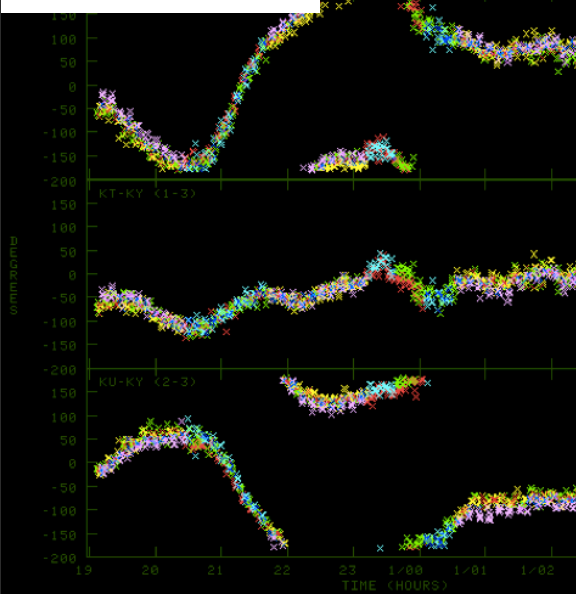
88 GHz, raw



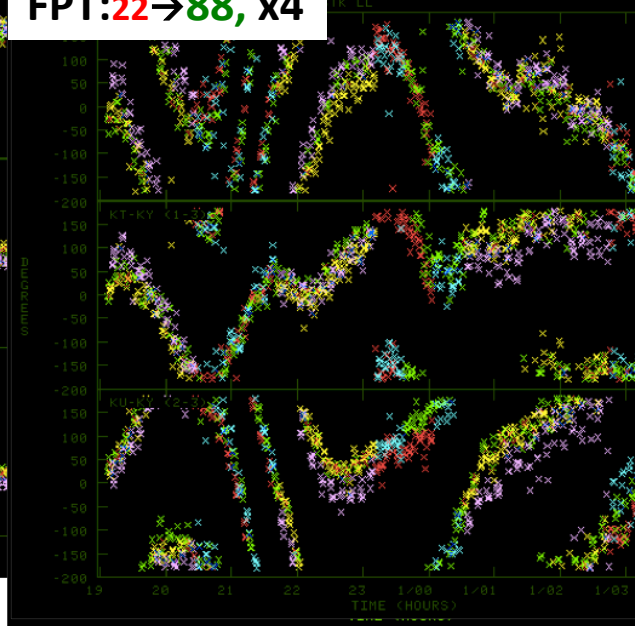
132 GHz, raw



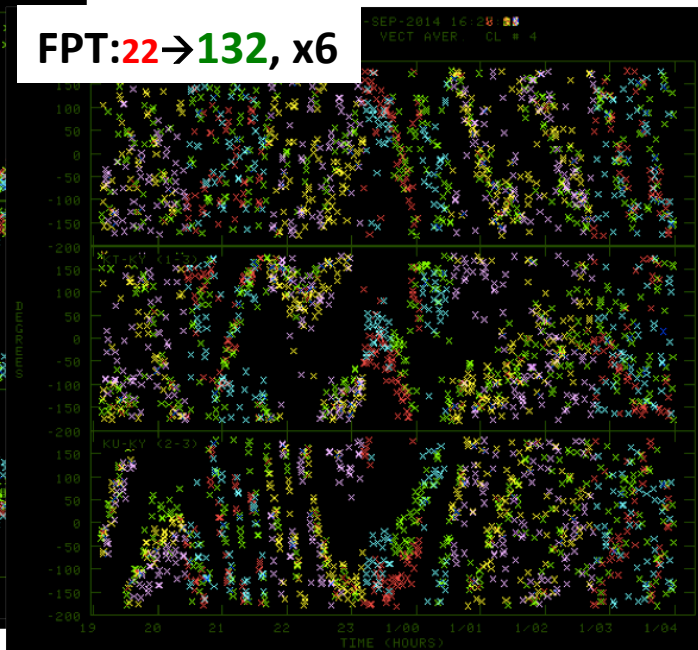
FPT:22→44, x2



FPT:22→88, x4



FPT:22→132, x6



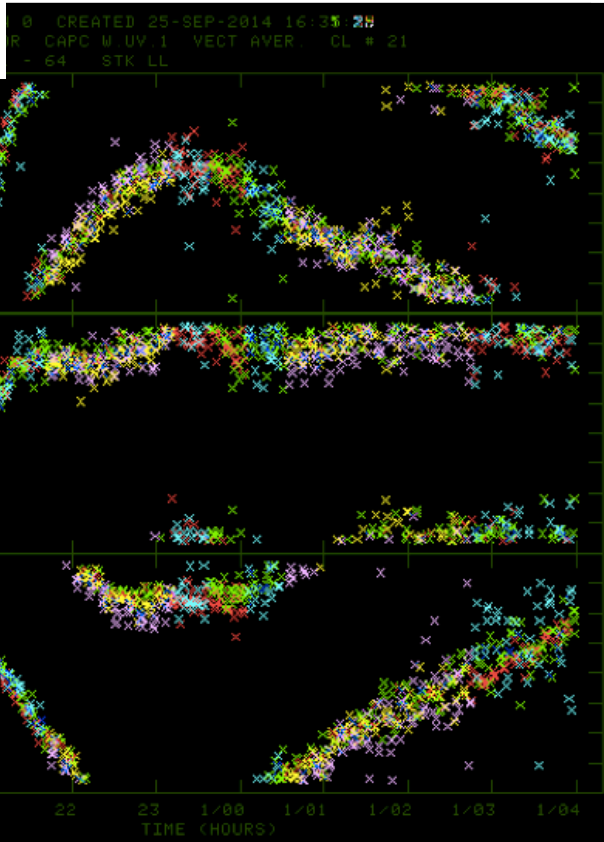




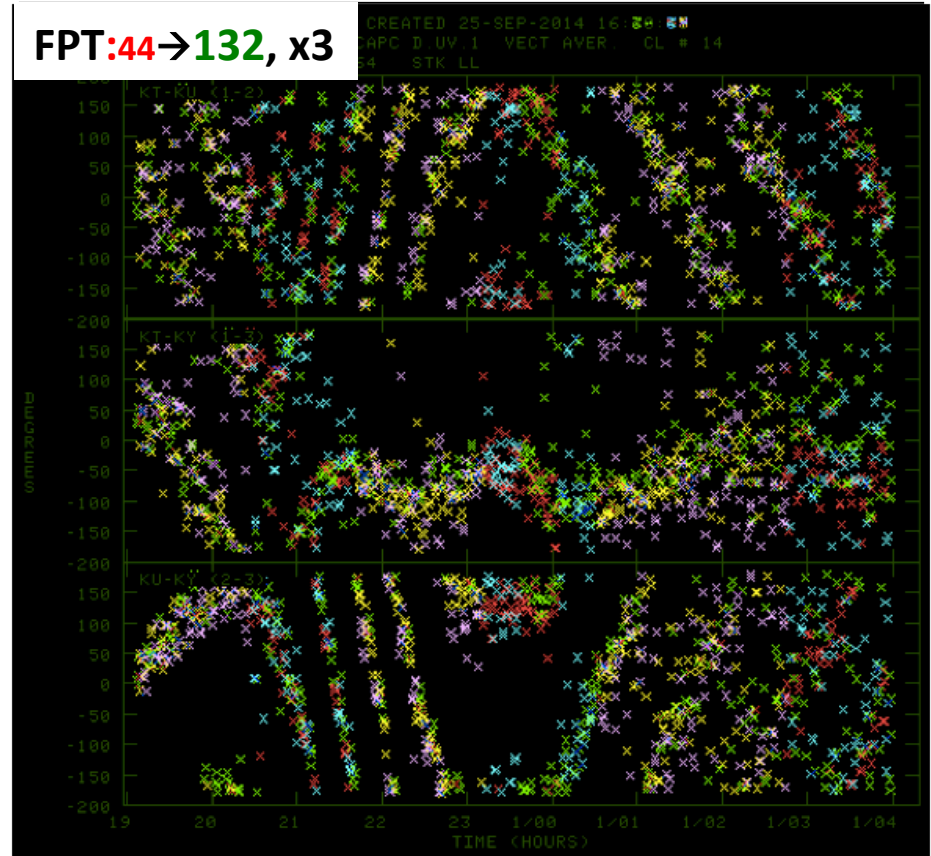
# FPT analysis – “2-frequencies”

Residuals increase with R, for a given  $\nu_{\text{low}}$  (44 GHz)

FPT:44→88, x2



FPT:44→132, x3

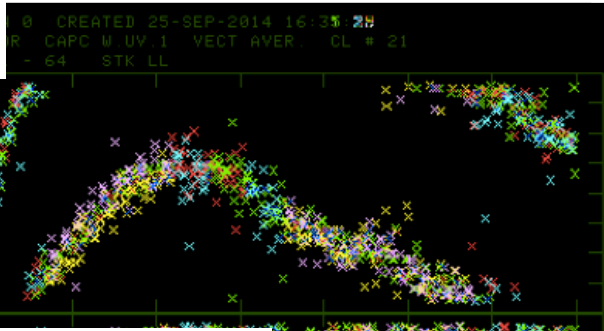




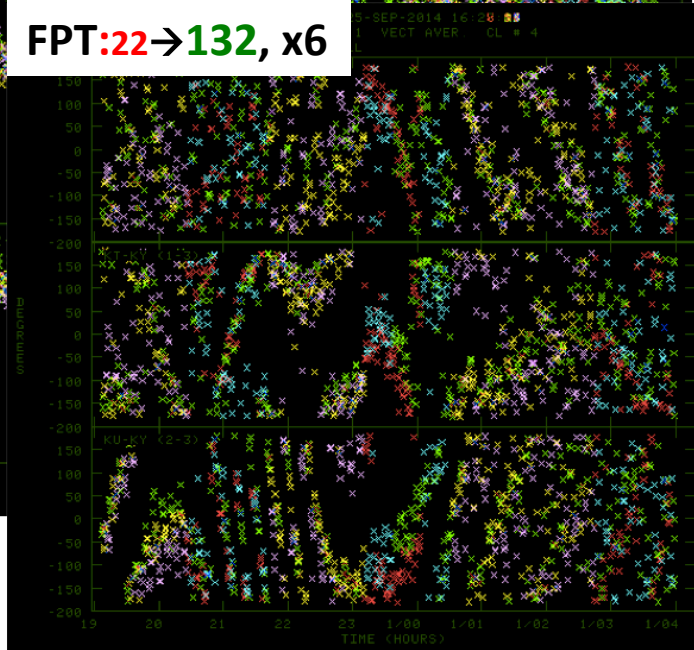
# FPT analysis – “2-frequencies”

Residuals increase with R, for a given  $\nu_{\text{low}}$  (44 GHz)

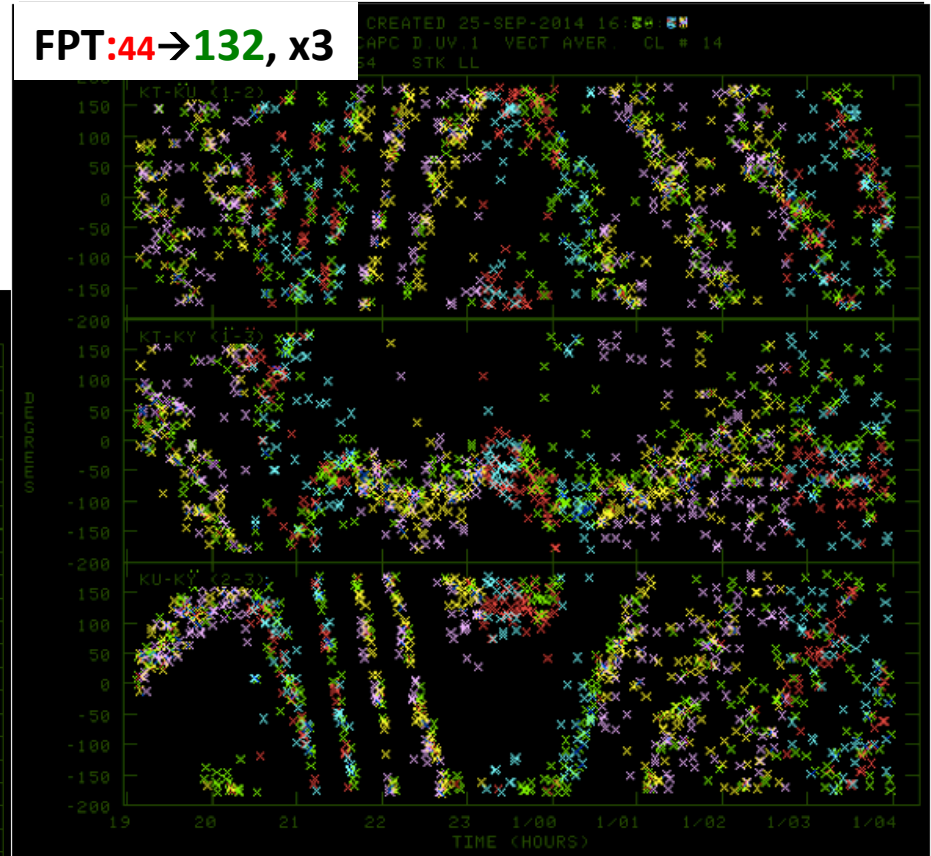
FPT:44→88, x2



FPT:22→132, x6



FPT:44→132, x3

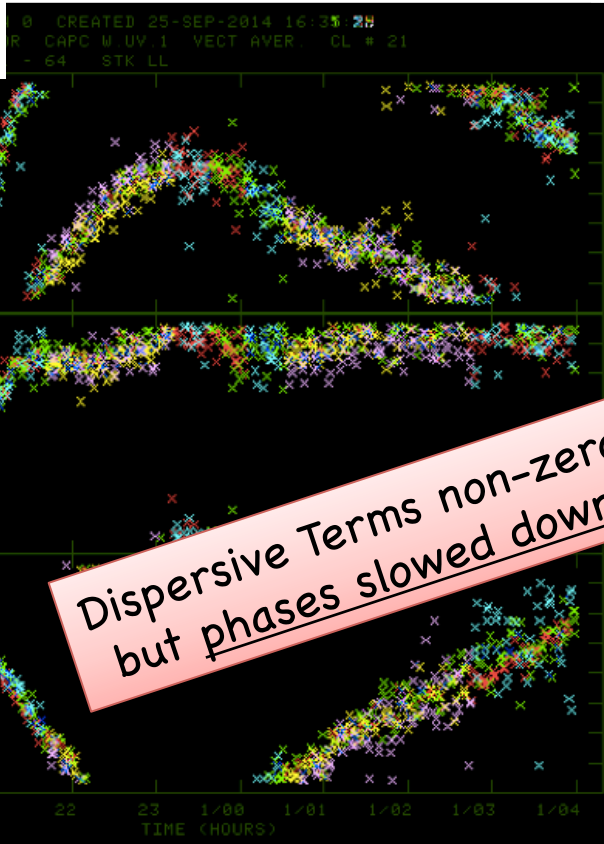




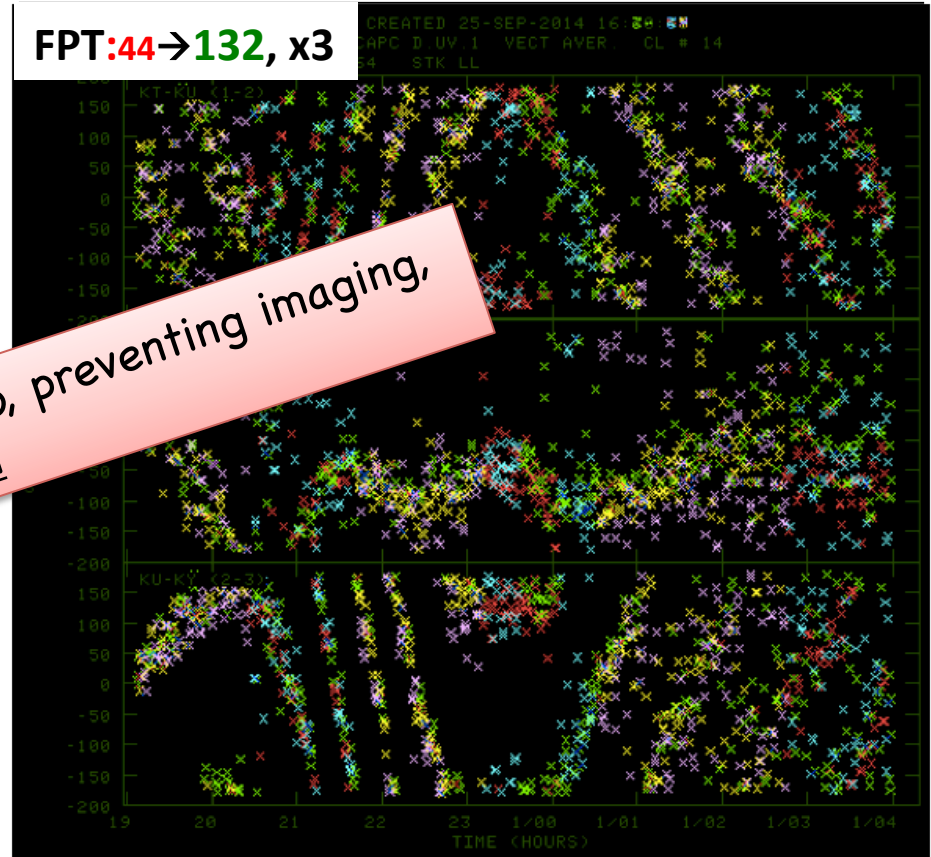
# FPT analysis – “2-frequencies”

Residuals increase with R, for a given  $\nu_{\text{low}}$  (44 GHz)

FPT:44→88, x2



FPT:44→132, x3



Dispersive Terms non-zero, preventing imaging,  
but phases slowed down

$$R = \nu / \nu_{\text{low}}$$

Fast    Slow    Slow


$$\phi_A^{\text{FPT}} = \cancel{\phi_{A,\text{GEO}}} + \cancel{\phi_{A,\text{TRO}}} + \phi_{A,\text{ION}} + \phi_{A,\text{INST}} + \phi'_{A,\text{STR}} + 2\pi n_A$$

$$R * \phi_A = R * (\phi_{A,\text{GEO}} + \phi_{A,\text{TRO}} + \phi_{A,\text{ION}} + \phi_{A,\text{INST}} + \widehat{2\pi n_A})$$



# Empirical Demonstration: 4-band KVN SFPR observations of 5 AGNs

(1) Outcomes: Effective Tropospheric Compensation  
**FPT analysis – “2-frequencies”**

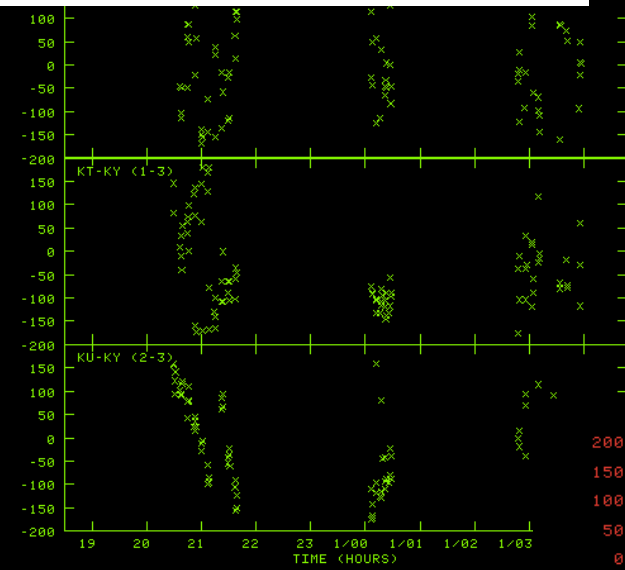


(2) Outcomes: Astrometry  
**SFPR analysis – “2-frequencies” & “2 sources”**

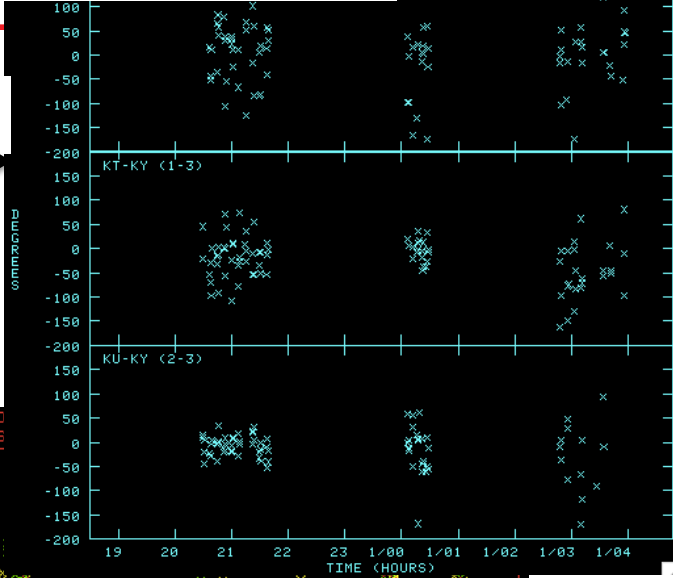


# SFPR analysis – 132 GHz with 43GHz: 2007+777 (ref. 6.3° away)

A) 2007+777, FPT, 44→132, x3

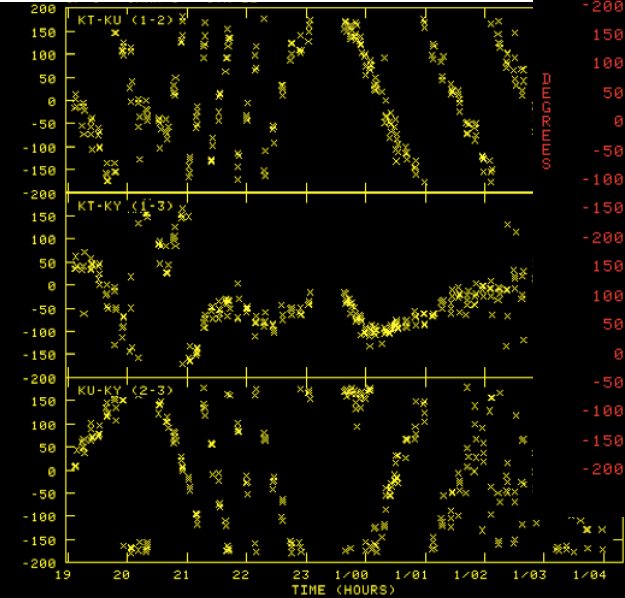


A) SFPR, 132 GHz

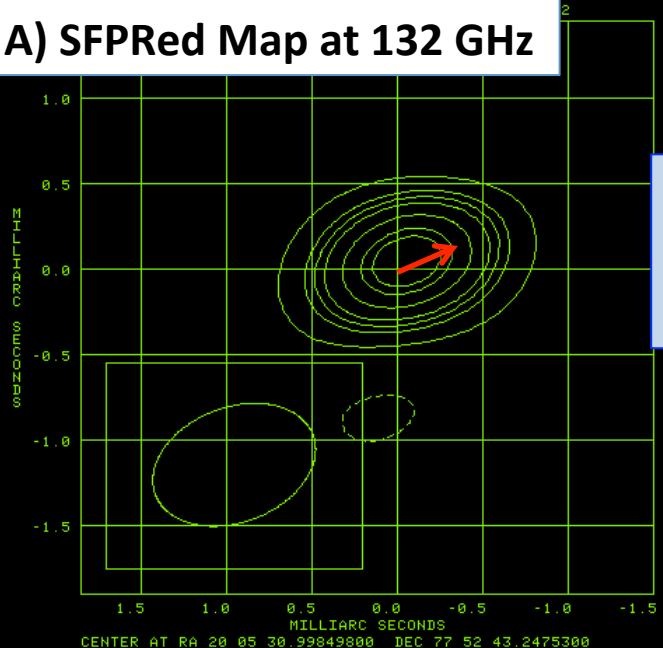


A) - B)

B) 1803+784, FPT, 44→132,



A) SFPRed Map at 132 GHz



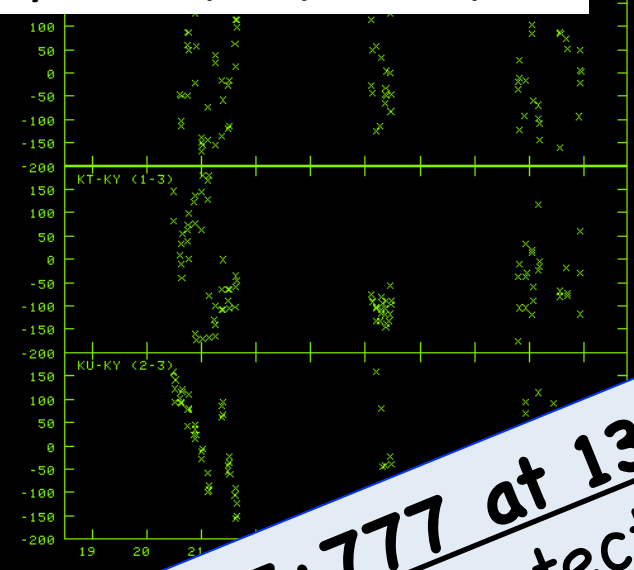
FFT

Peak Flux ~ 150 mJy  
rms ~ 5mJy/beam  
85-90% Flux Recovery

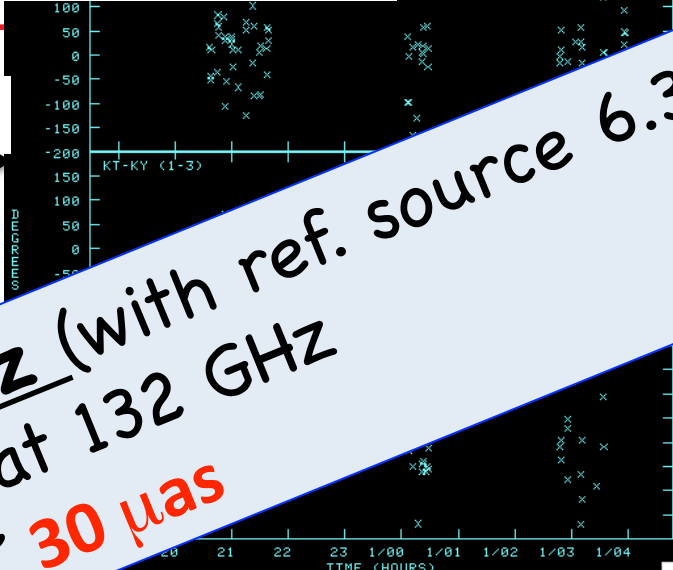


# SFPR analysis – 132 GHz with 43GHz: 2007+777 (ref. 6.3° away)

A) 2007+777, FPT, 44→132, x3



A) SFPR, 132 GHz

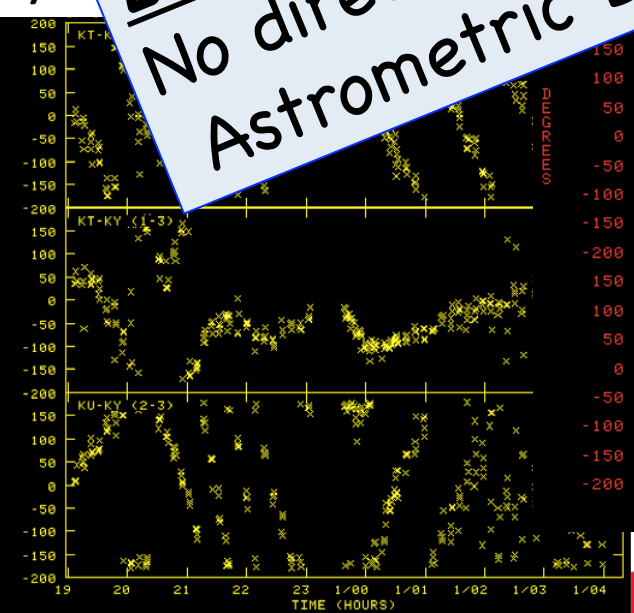


A) - B)

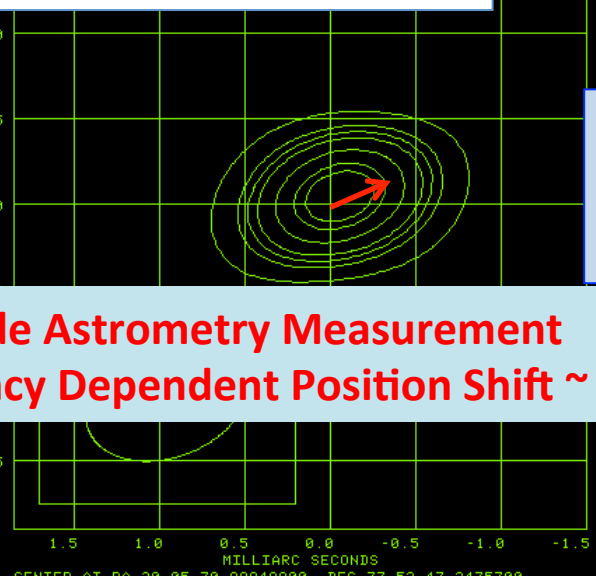


**2007+777 at 132 GHz** (with ref. source 6.3° away)  
**No direct detections at 132 GHz**  
**Astrometric Error ~ 30 μas**

B) 18



A) SFPRed Map at 132 GHz



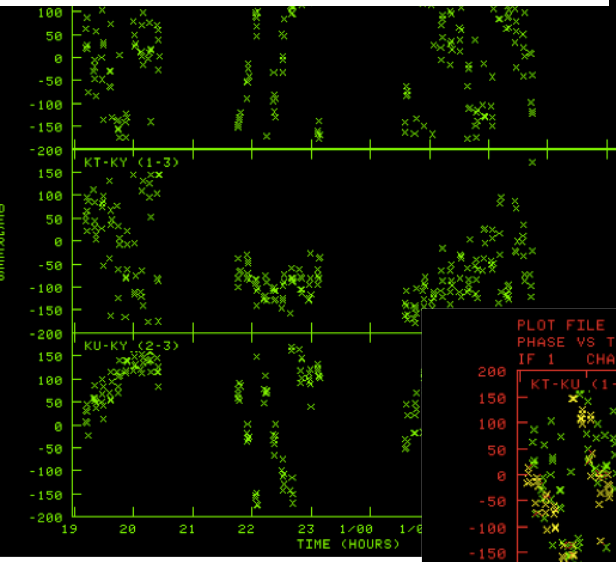
FFT

Peak Flux ~ 150 mJy  
 rms ~ 5mJy/beam  
 85-90% Flux Recovery

**Bona-fide Astrometry Measurement**  
**Frequency Dependent Position Shift ~ (-50,+50) μas**

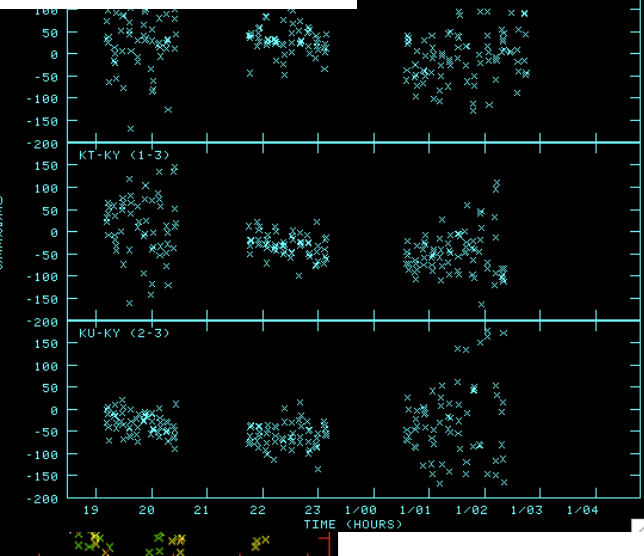
# SFPR analysis – 132 GHz with 43GHz: 1842+681 (ref. 11° away)

A) 1842+681 FPT,44→132, x3

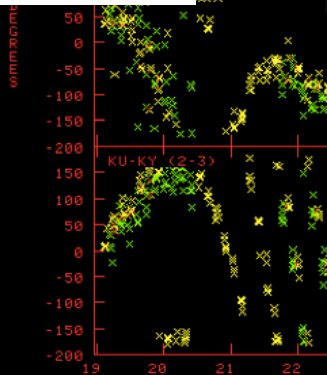
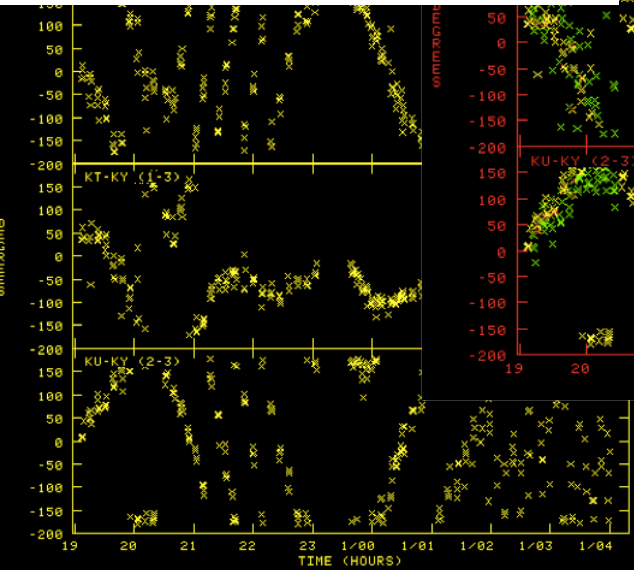


A) - B)

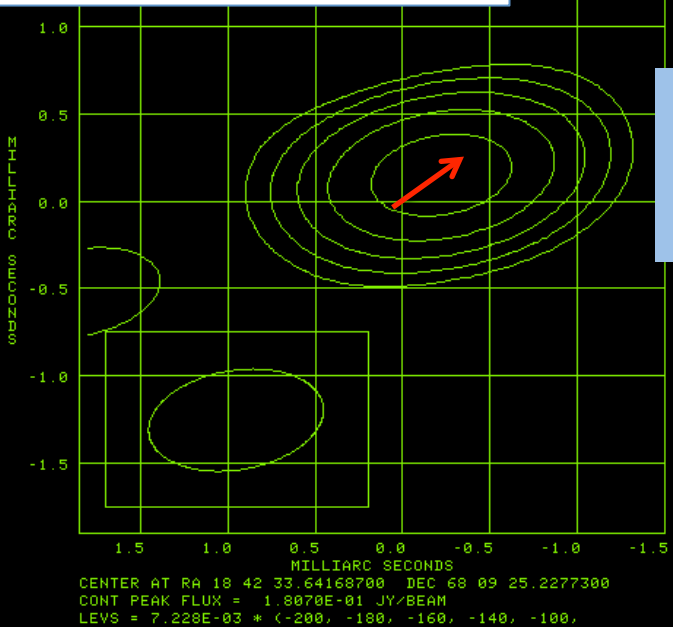
A) SFPR 132 GHz



B) 1803+784, FPT,44→132, x3



A) SFPRed Map at 132 GHz

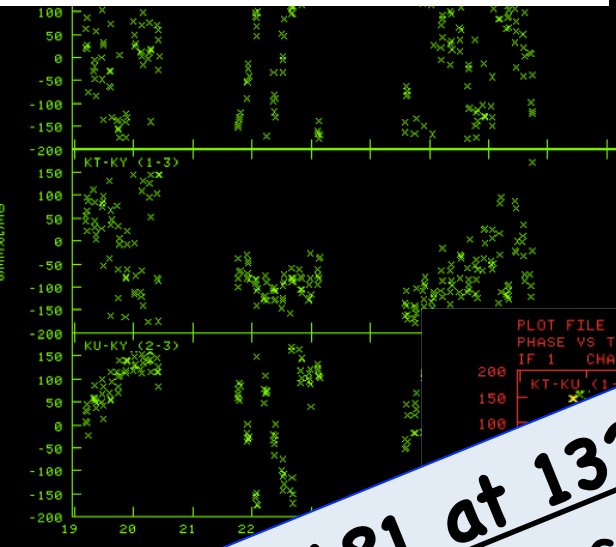


Peak Flux ~ 100 mJy  
rms ~ 5 mJy/beam  
87% Flux Recovery

FFT

# SFPR analysis – 132 GHz with 43GHz: 1842+681 (ref. 11° away)

A) 1842+681 FPT,44→132, x3



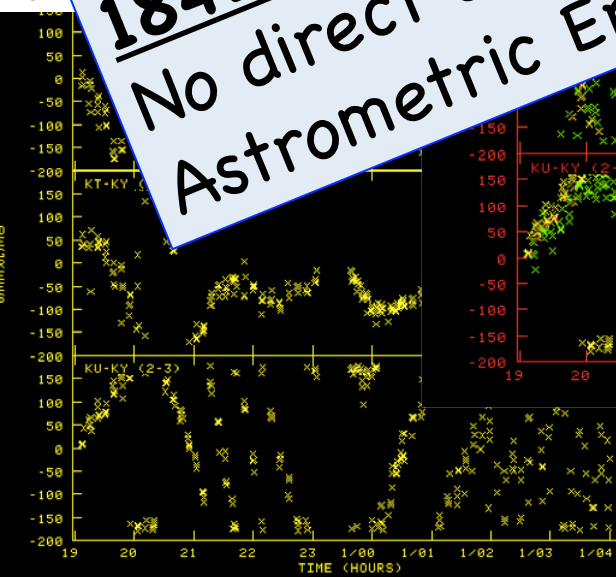
A) SFPR 132 GHz



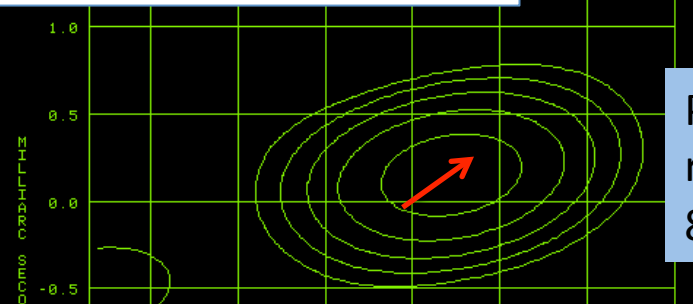
A) - B)

1842+681 at 132 GHz (with ref. source 11° away)  
 No direct detections at 132 GHz  
 Astrometric Error ~ 50 μas

B) 1842+681

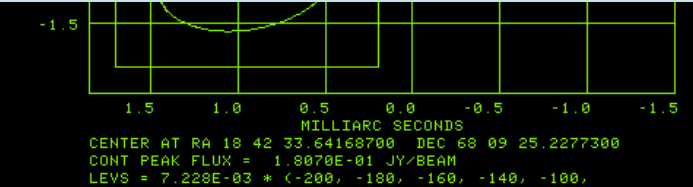


SFPRed Map at 132 GHz



Peak Flux ~ 100 mJy  
 rms ~ 5 mJy/beam  
 87% Flux Recovery

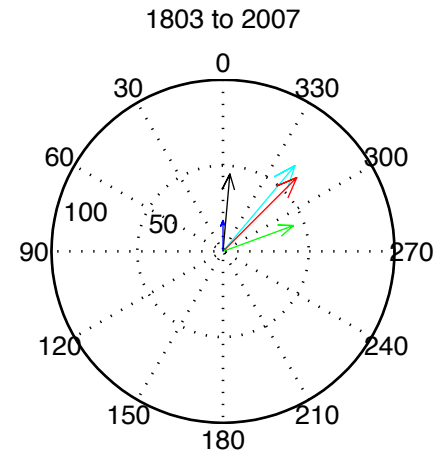
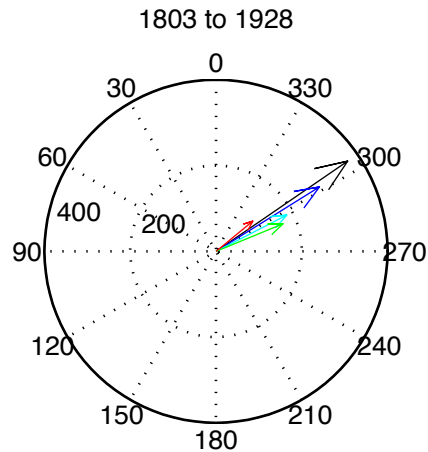
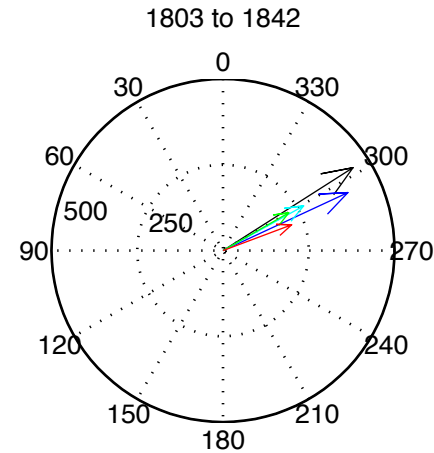
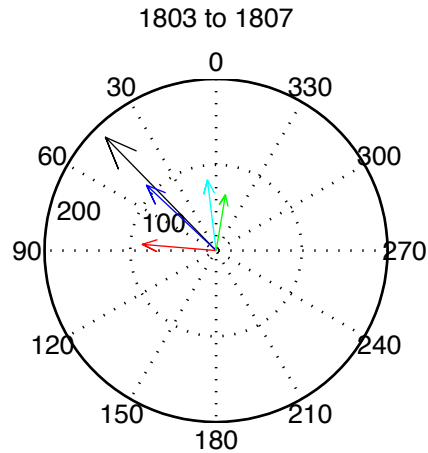
Bona-fide Astrometry Measurement  
 Frequency Dependent Position Shift ~ (-221,+150) μas



FFT



# SFPR Astrometric RELATIVE Measurements: between TWO frequencies & TWO sources



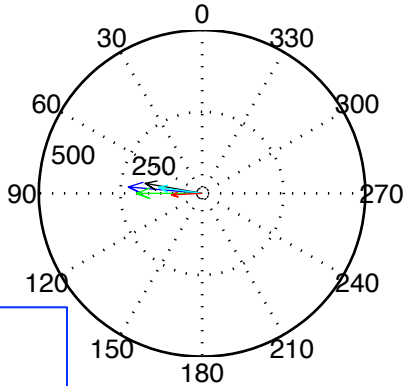
Red-KQ  
Blue KW  
Black KD  
Green QW  
Cyan QD

# Individual Source Shifts: Singular Value Decomposition Method PLUS Alignment with Jet Direction Constraint

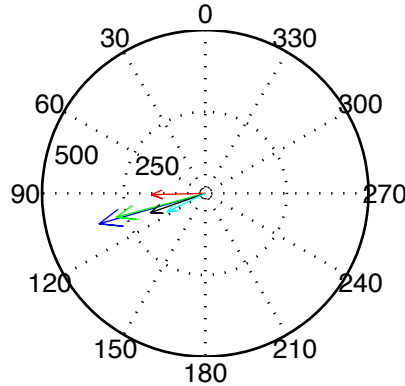


Non-Degenerate Solution

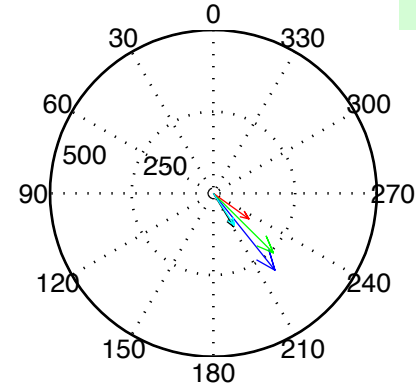
1803+784



1807+698

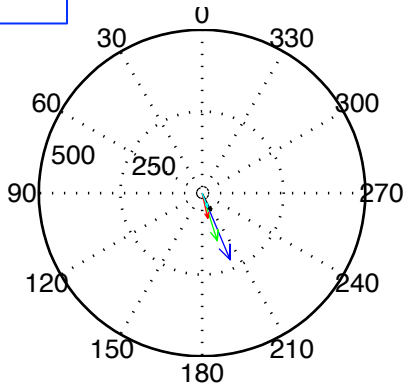


1842+681

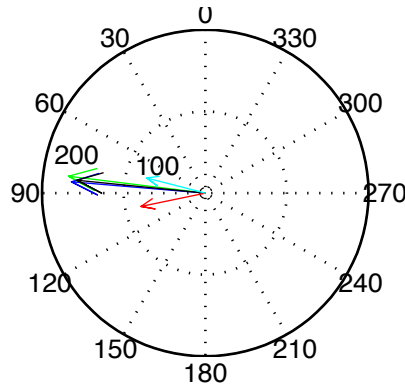


Red KQ  
Blue KW  
Cyan KD  
Green QW  
Black QD

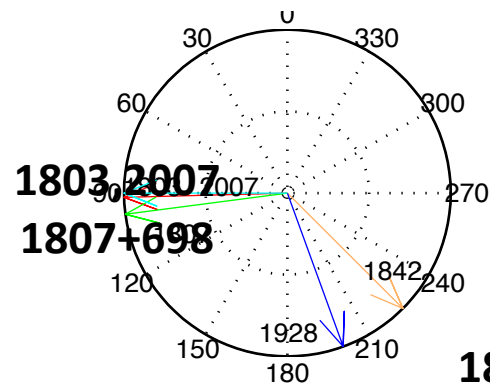
1928+738



2007+777



Jet Directions



1842+681

1928+738



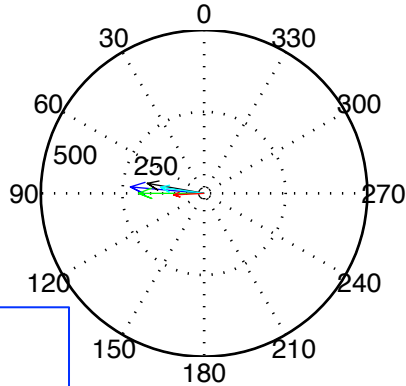


# Individual Source Shifts: Singular Value Decomposition Method PLUS Alignment with Jet Direction Constraint

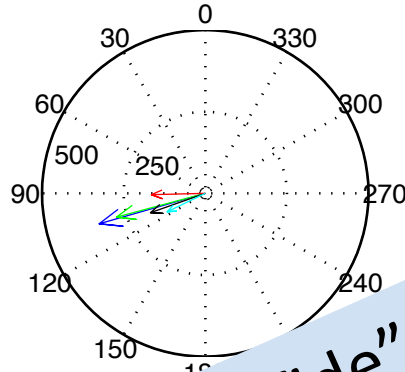


Non-Degenerate Solution

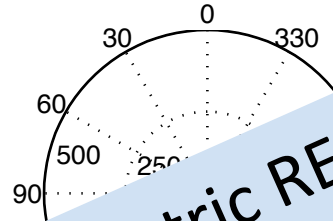
1803+784



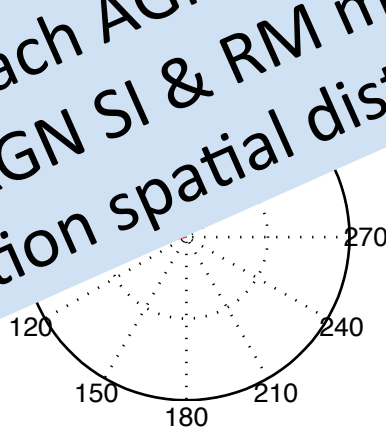
1807+698



1842+681



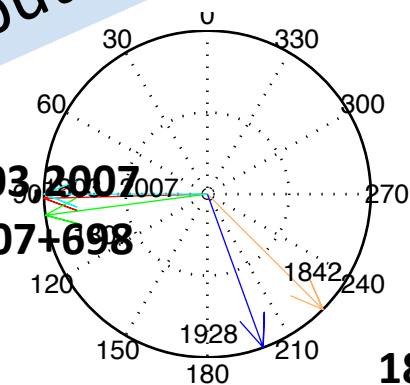
1928+738



1803+784

1807+698

Directions



1842+681

1928+738

- Red KQ
- Blue KW
- Cyan KD
- Green QW
- Black QD

Absolute Position Shifts for “bona fide” astrometric REGISTRATION of the images of each AGN at the four frequency bands. For spectral studies: AGN SI & RM maps, core-shifts, CSE/SF maser transition spatial distribution...






# Empirical Demonstration: 4-band KVN SFPR observations of 5 AGNs

(1) Outcomes: Effective Tropospheric Compensation  
**FPT analysis – “2-frequencies”**

(2) Outcomes: Astrometry  
**SFPR analysis – “2-frequencies” & “2 sources”**

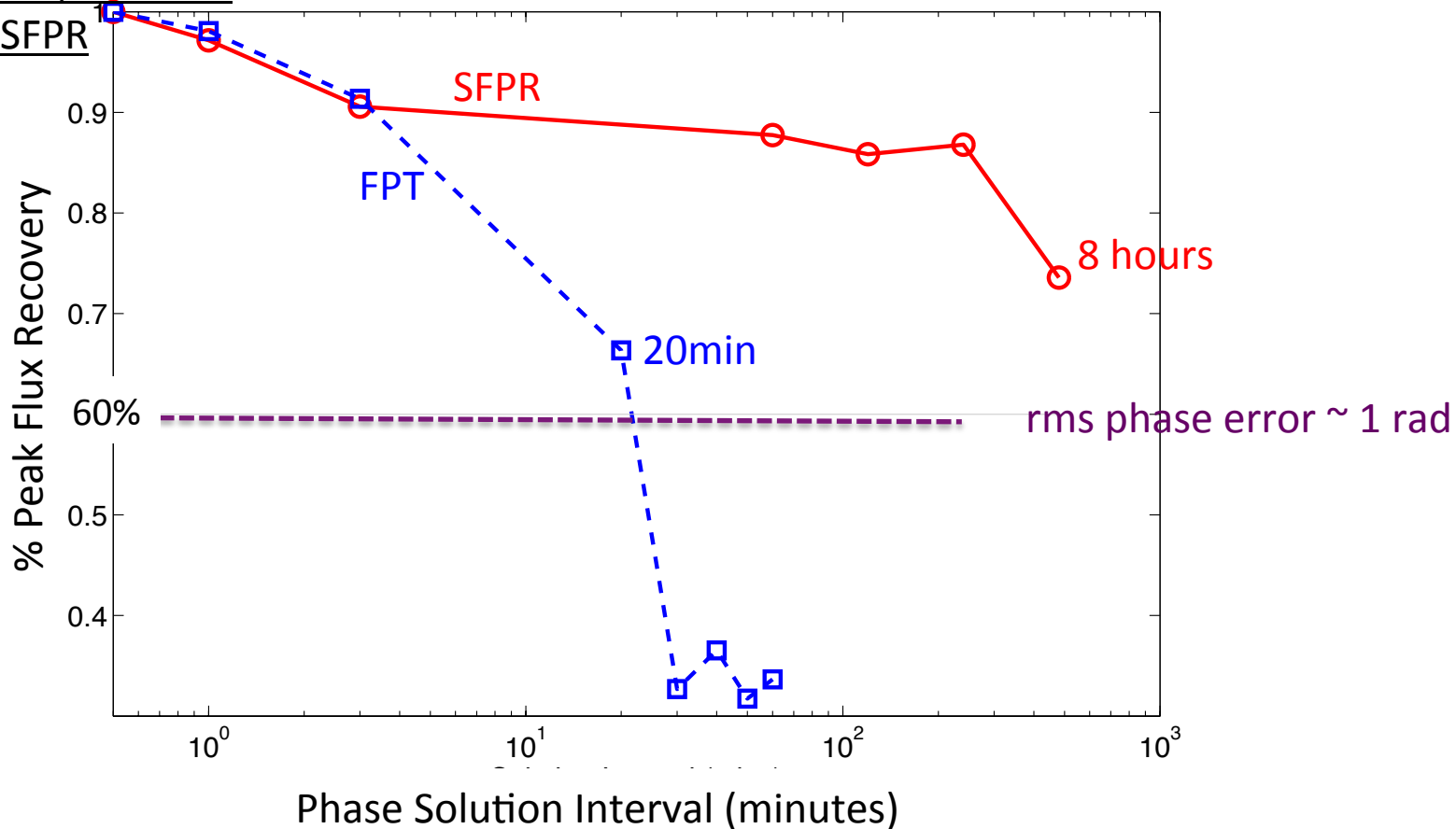
 (3) Outcomes: Increased Coherence Time  
**FPT & SFPR analysis**



# Empirical Demonstration: Coherence Studies at 130 GHz

Dataset: 1842+681, 130 GHz

Analysis: FPT & SFPR



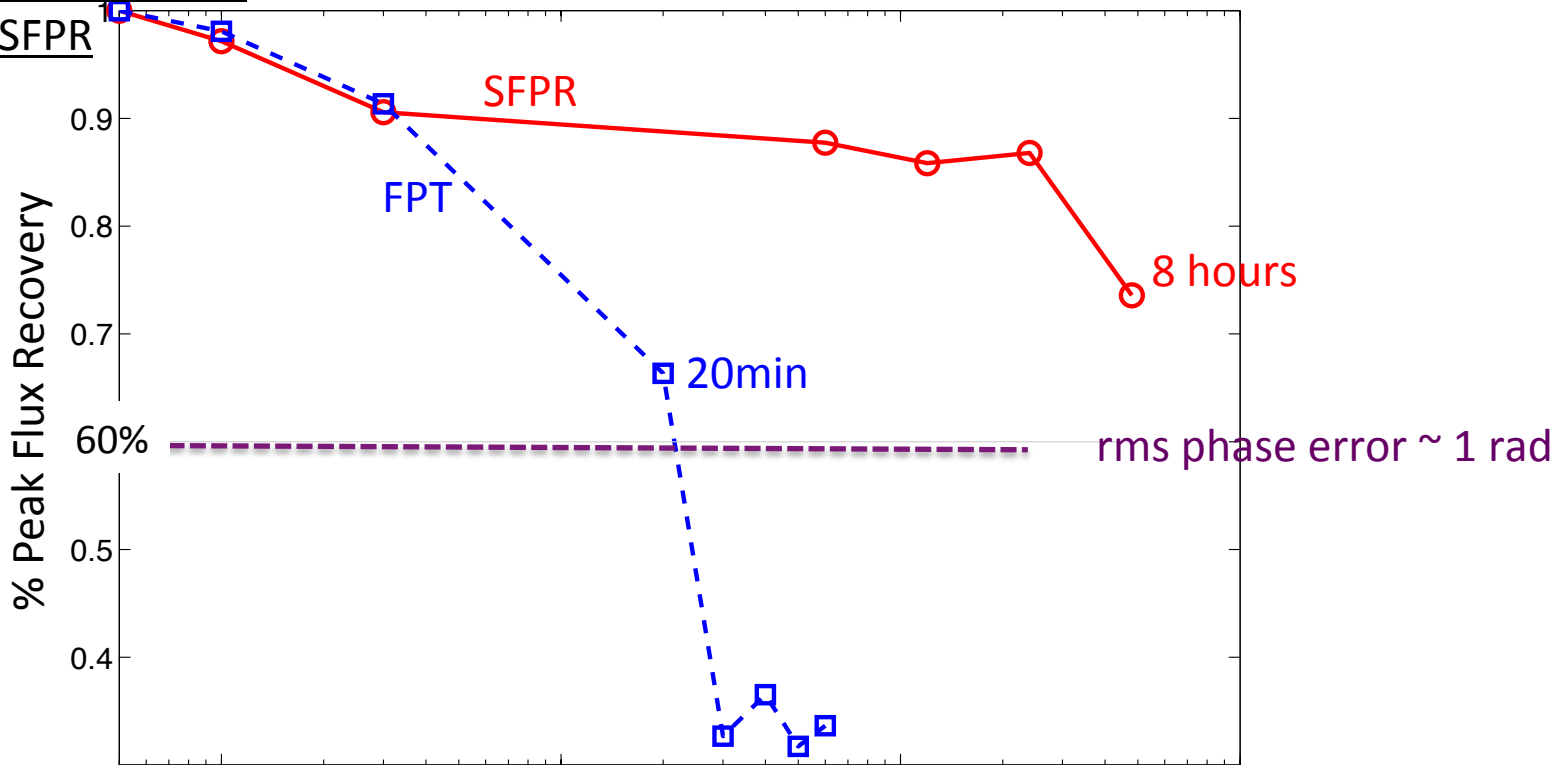
Freq.Pair	Analysis	Effective Coherence Time
44 → 132 GHz	FPT	20 minutes
44 → 132 GHz	SFPR ( $\theta \sim 11\text{deg}$ )	> 8 hours



# Empirical Demonstration: Coherence Studies at 130 GHz

Dataset: 1842+681, 130 GHz

Analysis: FPT & SFPR



Typical Atmospheric Coherence Time @ 130 GHz ~ tens of seconds

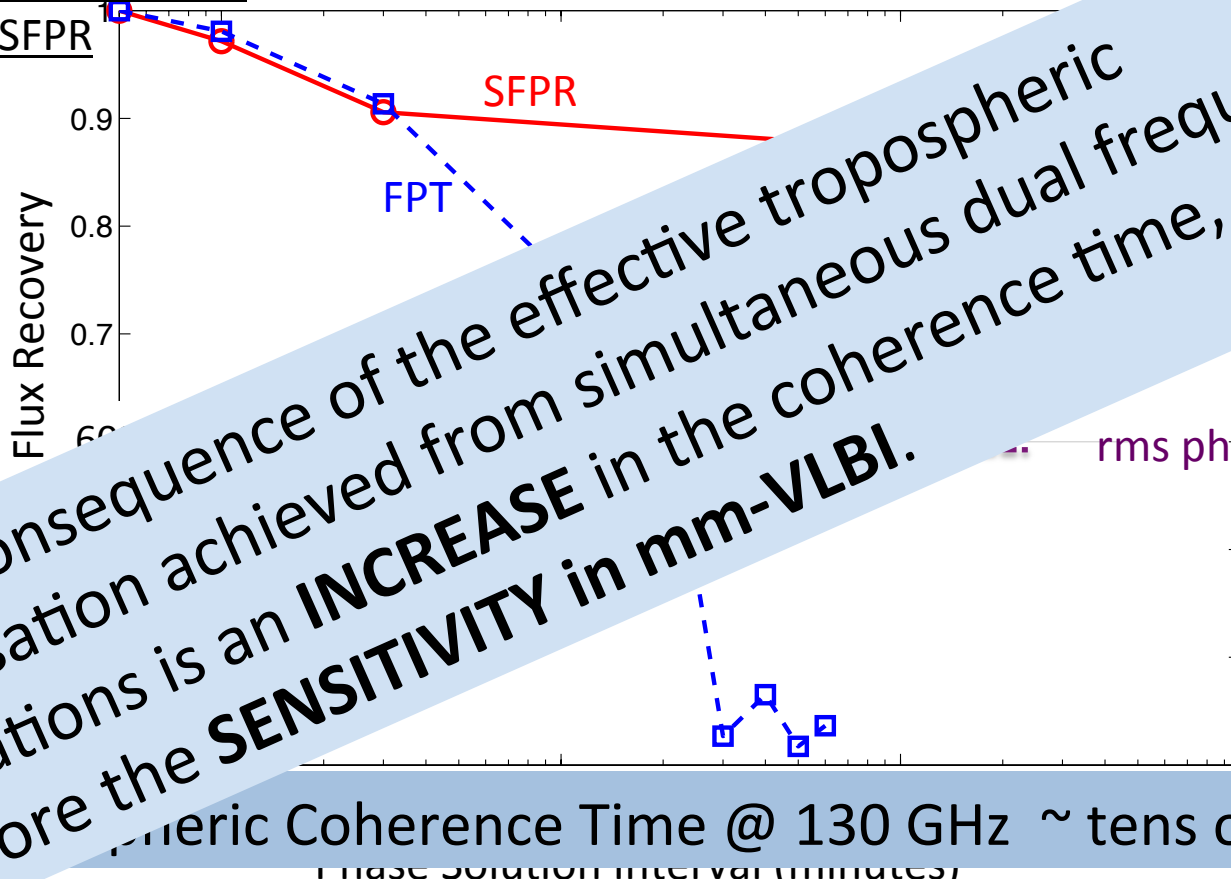
Freq.Pair	Analysis	Effective Coherence Time
44 → 132 GHz	FPT	20 minutes
44 → 132 GHz	SFPR ( $\theta \sim 11 \text{deg}$ )	> 8 hours



# Empirical Demonstration: Coherence Studies at 130 GHz

Dataset: 1842+681, 130 GHz

Analysis: FPT & SFPR



A direct consequence of the effective tropospheric compensation achieved from simultaneous dual frequency observations is an **INCREASE** in the coherence time, and therefore the **SENSITIVITY** in mm-VLBI.

Generic Coherence Time @ 130 GHz ~ tens of seconds

Eq. Pair	Analysis	Effective Coherence Time
44 → 132 GHz	FPT	20 minutes
44 → 132 GHz	SFPR ( $\theta \sim 11 \text{deg}$ )	> 8 hours





# Summary

Potential of multi-frequency observations to improve the performance of mm-VLBI

## SFPR enables:

- Superior tropospheric compensation, boost array with increased sensitivity.
- High precision astrometry at (sub-)mm-VLBI
- No upper frequency limit (B2B mode in ALMA at ca. 650 GHz)

Widely applicable, to many sources

Very effective use of observing time

Technology ready, Slow telescope switching

Empirical Demonstration with KVN observations up to 132 GHz:

First time astrometric measurements made at 130 GHz

Coherence time extended to 20 minutes (FPT) or greater than 8 hours (SFPR)

## Astrophysical applications:

- Multi-frequency studies with “bona fide” astrometric registration, in continuum and spectral line observations.
- Weak Sources



# Work in Progress – What's next?

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**Network: International Baselines (KVN Pilot Project) (Tuesday morning)**  
**(long baselines highly desirable for increased astrometric precision, resolution)**

**Engineering: Possibilities for (near) simultaneous multi-frequency obs.**  
**(mid Tuesday)**

**Analysis: ICE Blocks for ionospheric calibration (alternative to SFPR)**  
**(today)**

**Unique Science Drivers (today):**

**AGNs, Evolved Stars / Star forming regions, weak sources.**  
**KVN applications to spectral line studies**

**Leading to General discussions with a forum of engineers and astronomers**  
**“How to establish a European Multi-Frequency Observatory”**  
**(end Tuesday)**



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**END**

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